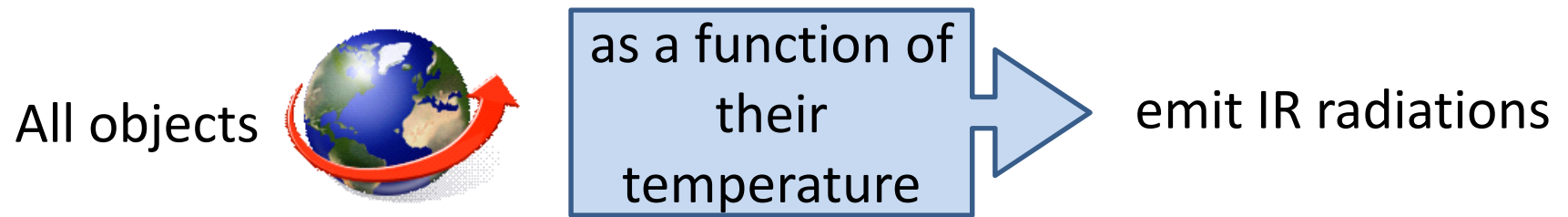


# Thermography

by: mahnaz Etehadtavakol



As an object gets hotter  more intense IR radiation

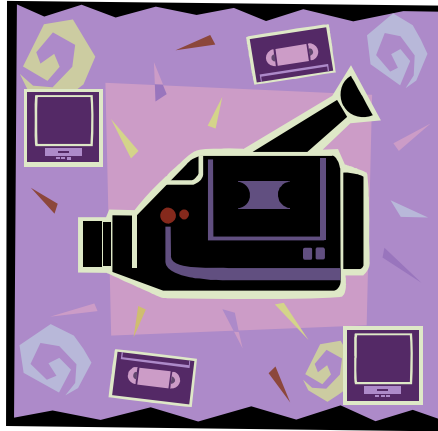
 shorter wavelength

$0.75 \mu\text{m} < \text{IR} < 300 \mu\text{m}$

$1 \text{ THZ} < \text{IR} < 430 \text{ THZ}$



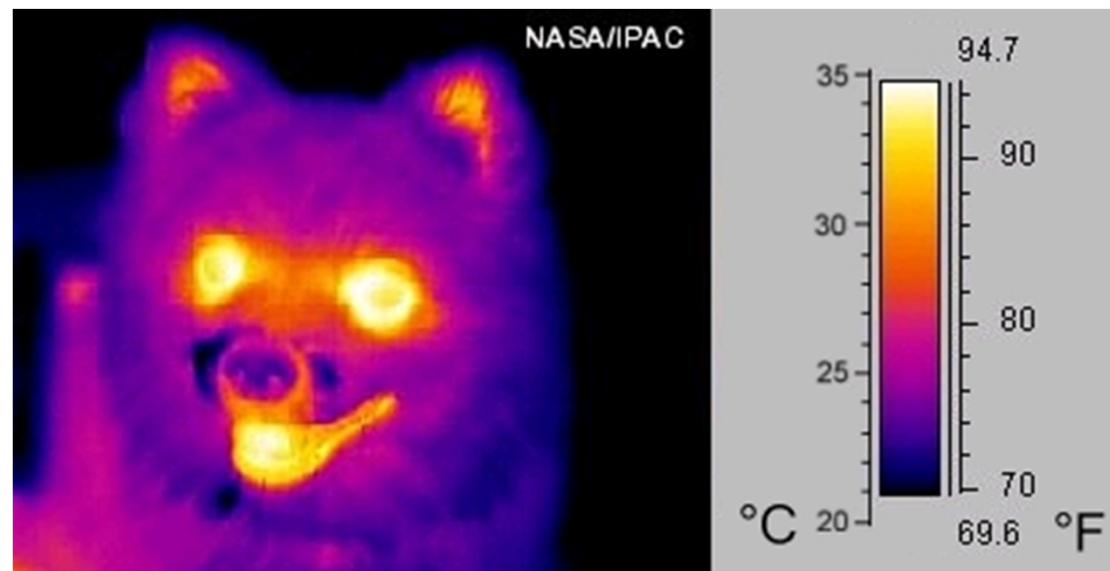
Thermal imaging



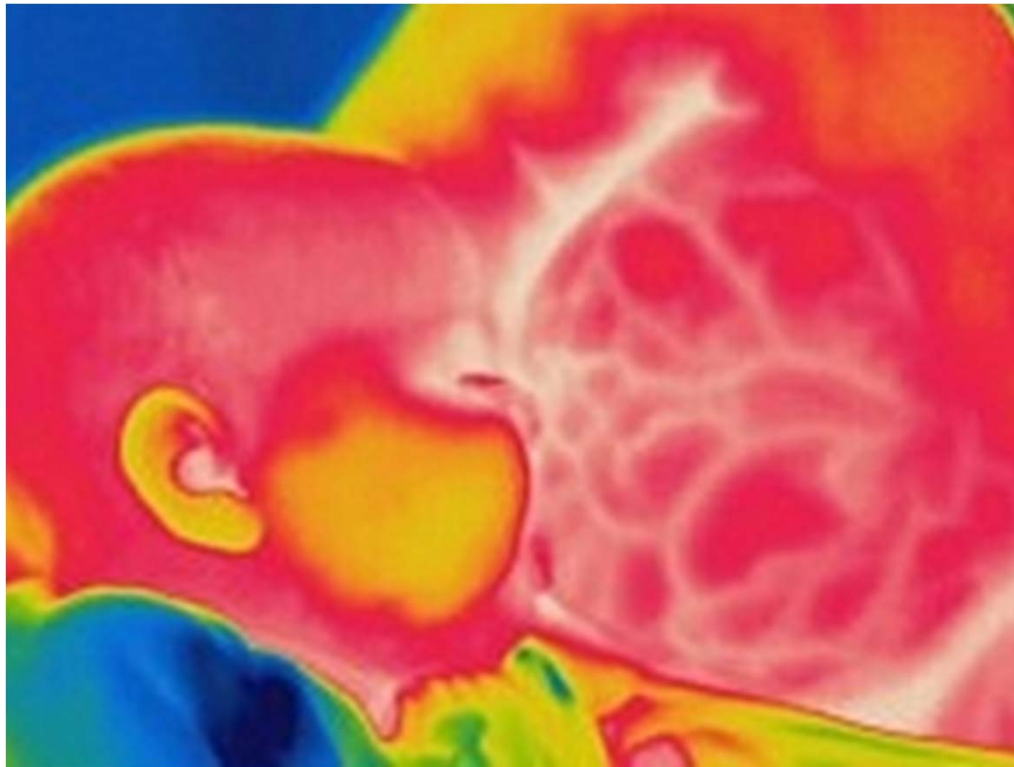
Can Detect



in the infrared range and produce thermograms



Thermography shows variations in temperature

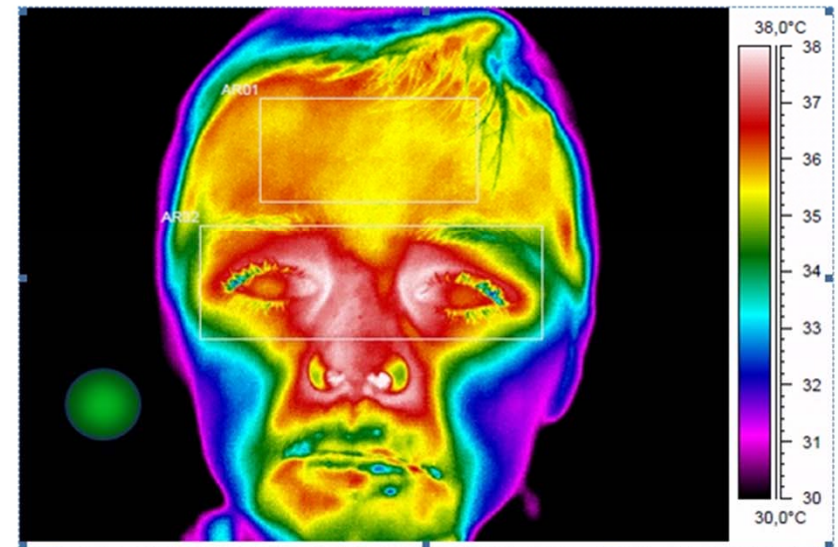




# Airport personnel used thermography suspected cases



during the 2009 pandemic

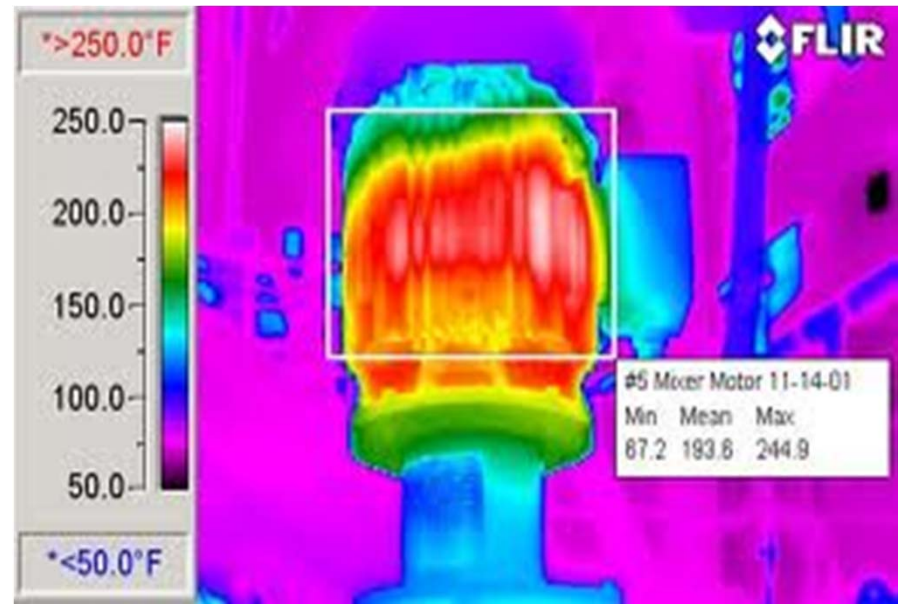


Subject 3 fever

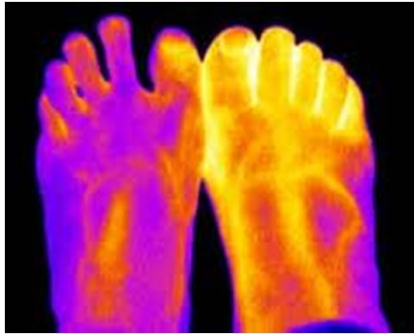
# Application of thermography



Fire rescue



Motor inspection



Oncology-feet

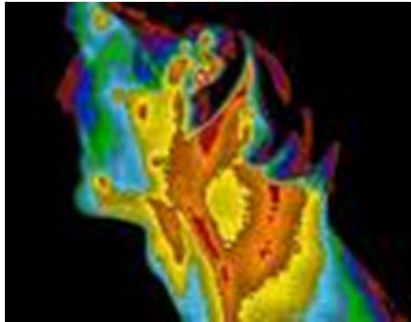


Multiple Sclerosis



whiplash

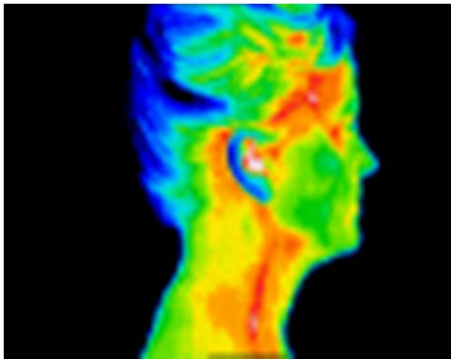
## Medical application



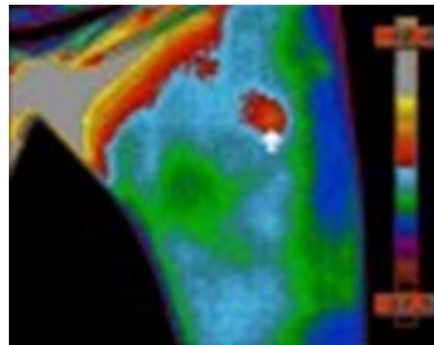
Pre stroke



Breast cancer



headache



Skin cancer



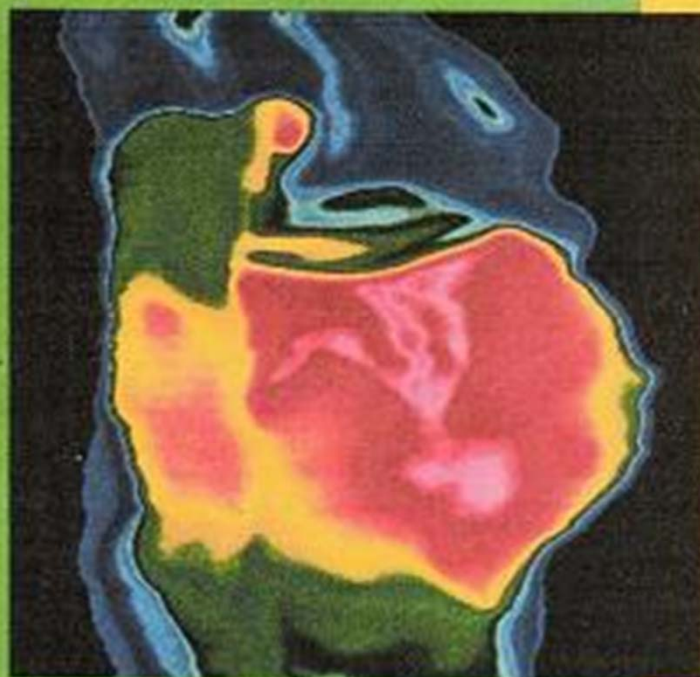
Whole body



# SCIENTIFIC COMPUTING & AUTOMATION

Volume 10 Number 4  
April 1988

April 1988

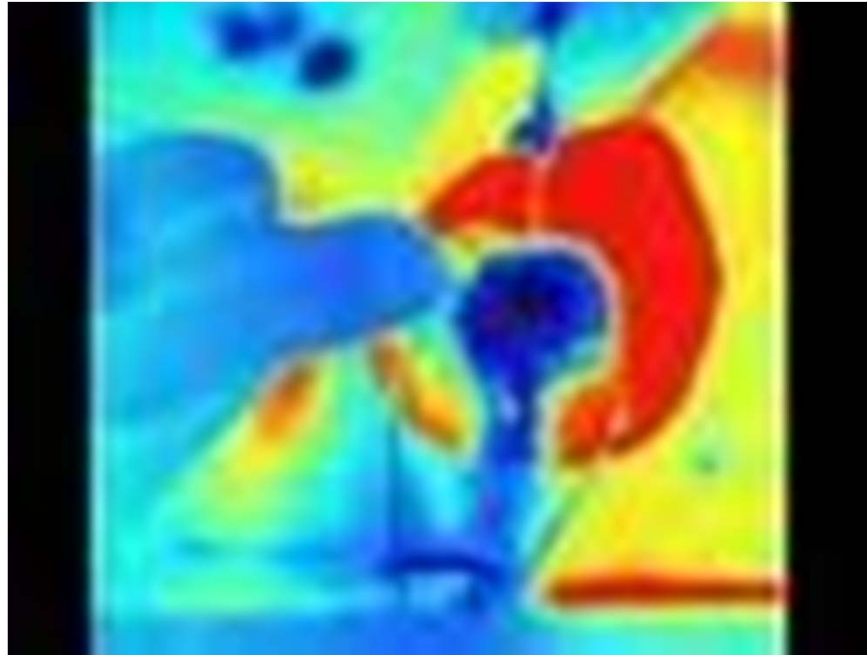


- Computerized Thermal Imagery
- Computational Chemistry in Research
- Experts Creating Expert Systems

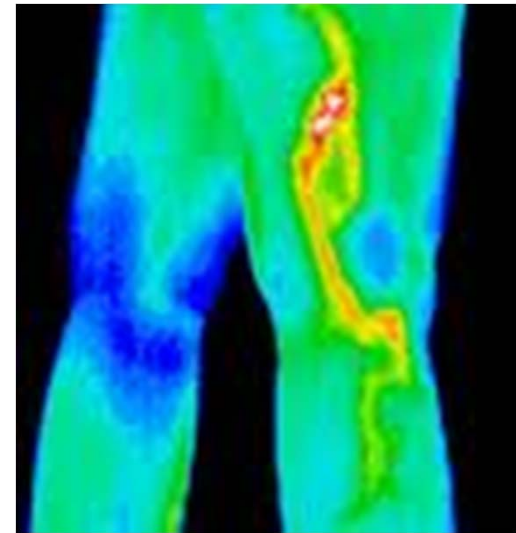
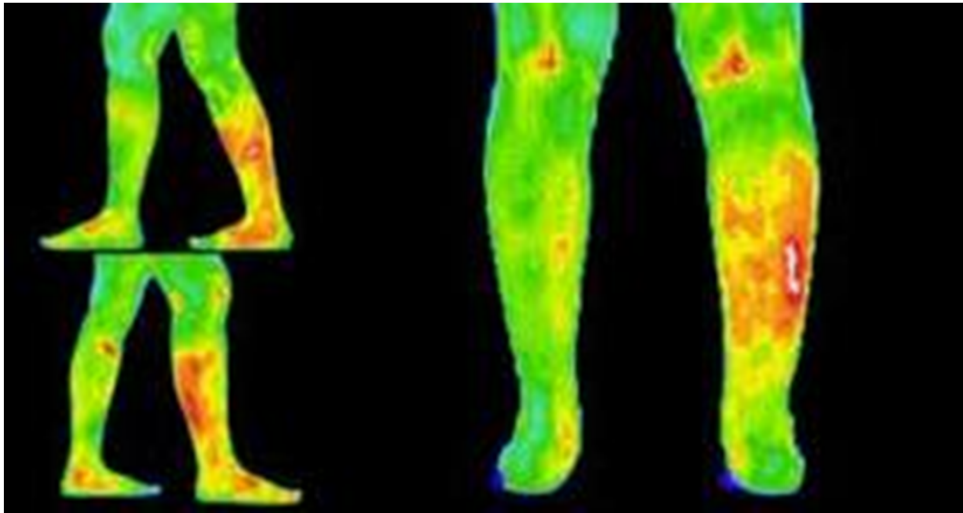
**BUYER'S GUIDE**  
Data Acquisition  
& Control

**PRODUCT PROFILE**  
Lab Integrators

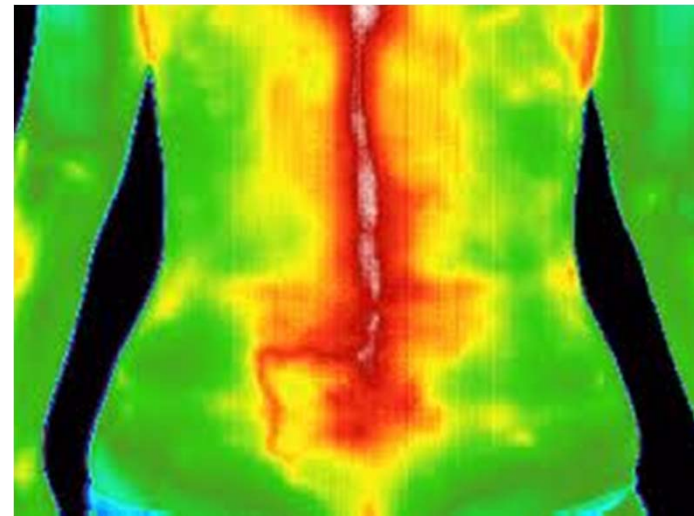
Published by  
McGraw-Hill, Inc.  
1221 Avenue of the Americas  
New York, NY 10020-1398



Thermography during surgery



Location of pain



# Breast thermography

- early detection
- non-invasive
- non-radiating
- passive
- fast
- painless
- low cost
- risk free
- no contact with the body
- women with all ages
- all sizes of breast
- fibrocystic breasts
- dense tissue
- pregnant
- nursing women
- portability
- real time imaging
- monitoring after surgery

*A normal breast thermogram for each woman  
is like her fingerprint*

*It's uniquely hers,*

*and it doesn't change much over time*



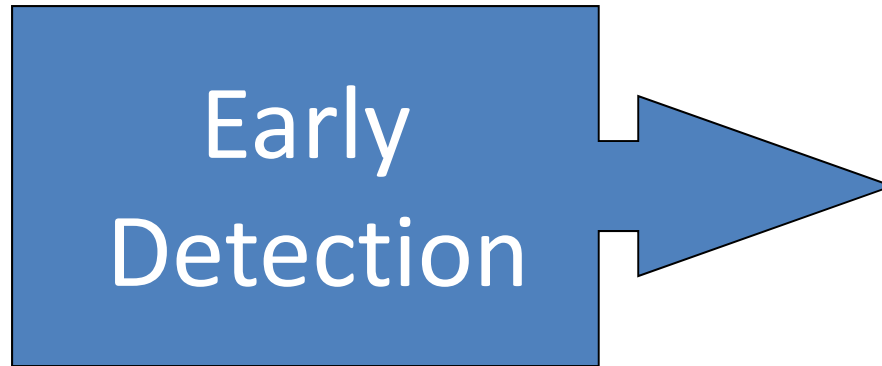
# Thermography vs. Mammography

Thermography  Physiological changes

Mammography  Anatomical changes

Physiological changes  Anatomical changes

Thermography complementary Mammography

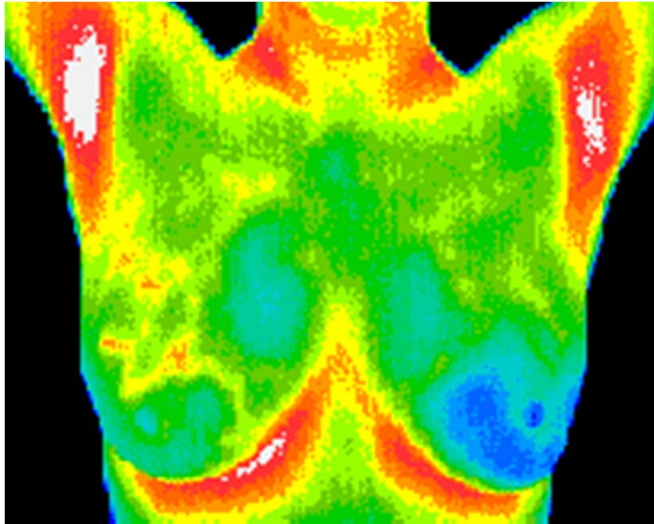


%85

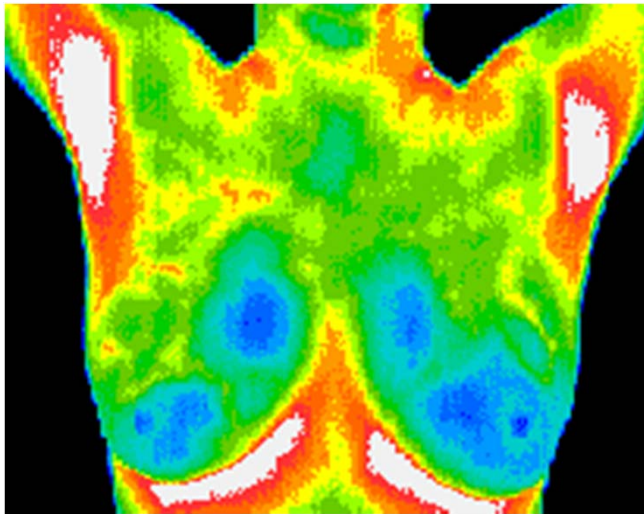
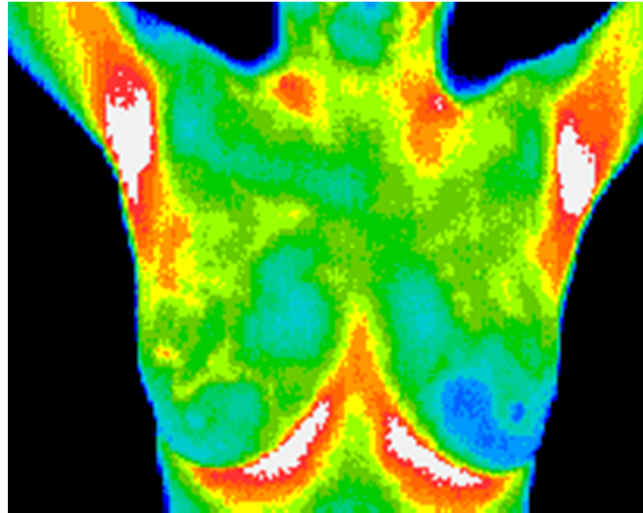


<http://yourtotalhealth.ivillage.com/thermography.html>  
] [www.earlycancerdetection.com/breast thermo.html](http://www.earlycancerdetection.com/breast_thermo.html)

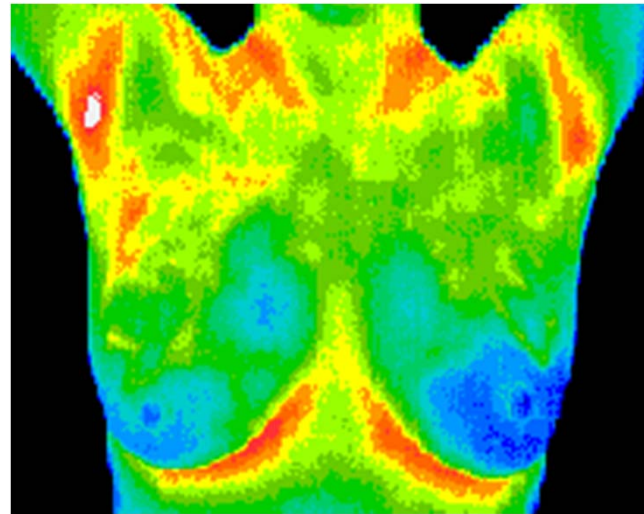
Baseline



3 month follow up

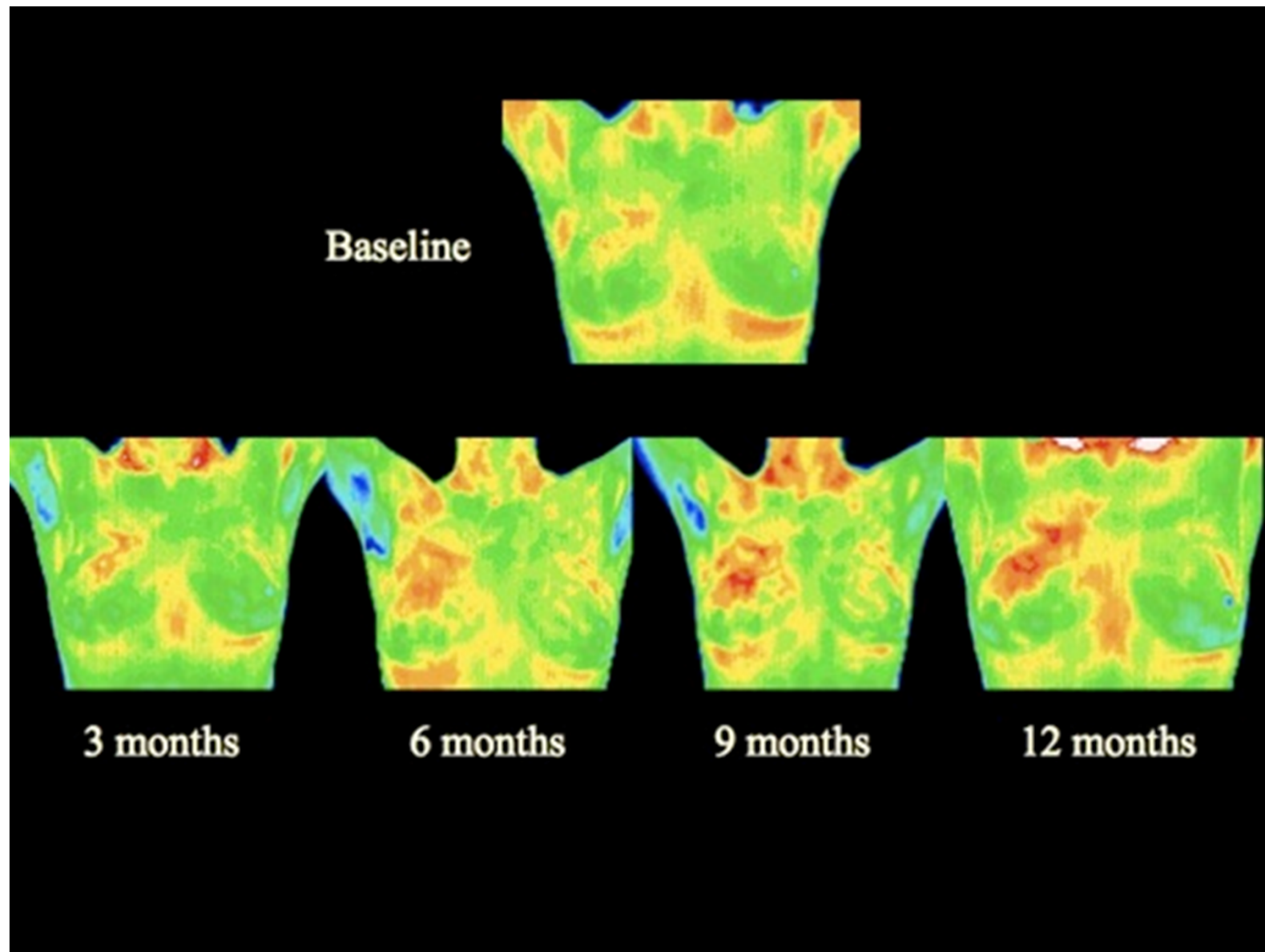


First annual



Second annual

**Healthy thermograms  
stable for two years**



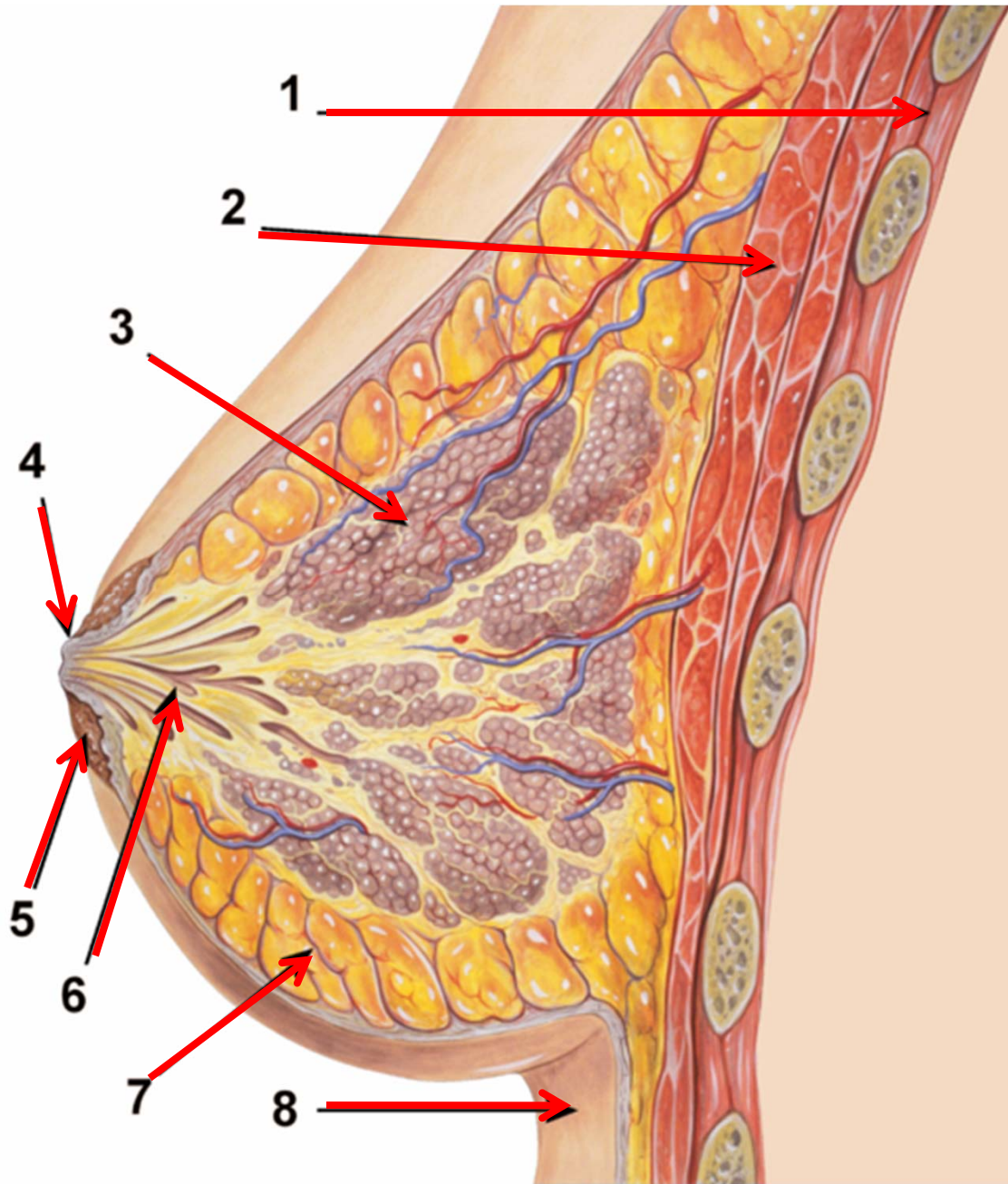
Ductal Carcinoma in Situ was not detectable by mammogram until final image

# Breast thermography

- In 1982 and again in 2005
- FDA
- breast thermography as an adjunctive breast screening

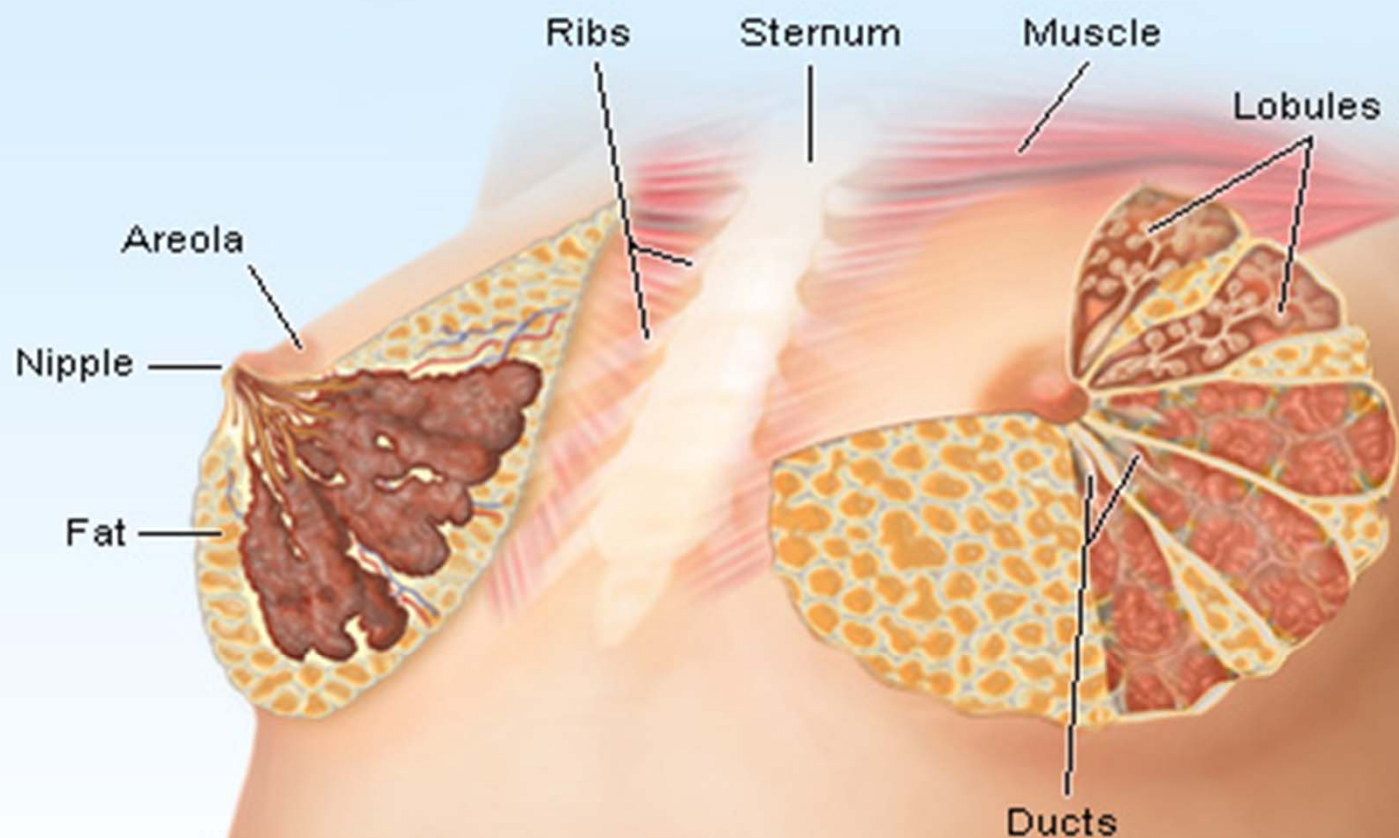


# Breast anatomy



1. Chest wall
2. Pectoralis muscles
3. Lobules
4. Nipple surface
5. Areola
6. Lactiferous duct
7. Fatty tissue
8. Skin

# Anatomy of the Breast



Sample Use Only - Copyrighted

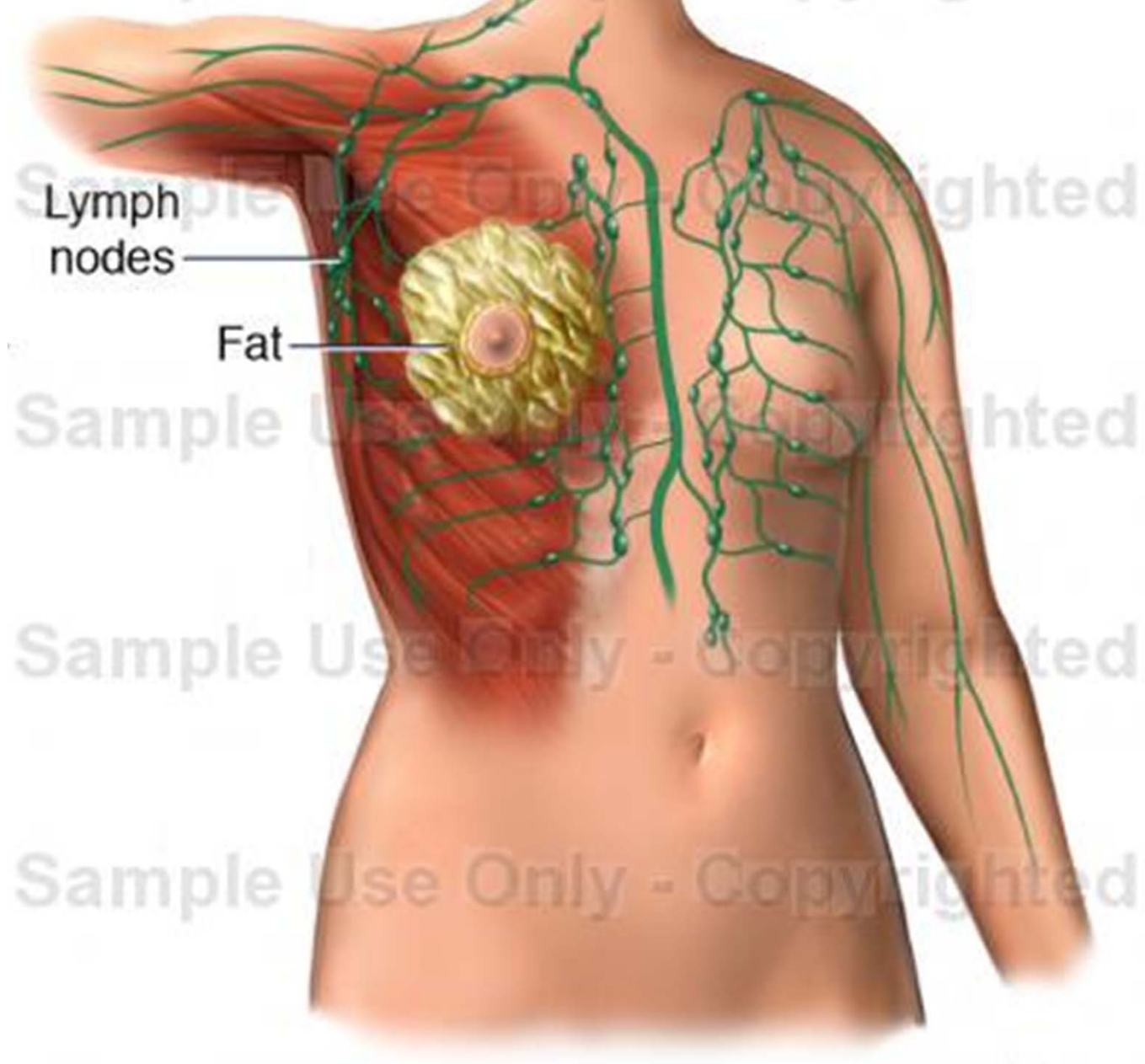
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# Entendiendo el cáncer de mama

## ¿Qué es el cáncer de mama?

El cáncer de mama es un tipo de cáncer que se desarrolla en la mama. El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal. El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal. El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal.

## Tipos de cáncer de mama

El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal. El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal. El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal.



Tumor de mama ductal in situ (DCIS)

Este tipo de cáncer de mama se desarrolla dentro de los ductos mamarios. Las células cancerosas se han acumulado dentro de los ductos, pero aún no se han extendido más allá de la pared del ducto.



Tumor de mama invasivo

Este tipo de cáncer de mama se desarrolla dentro de los ductos mamarios. Las células cancerosas se han extendido más allá de la pared del ducto y se han propagado a los tejidos circundantes.

## Antecedentes mamarios (AMM)

El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal. El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal. El cáncer de mama puede ser de diferentes tipos, pero el más común es el cáncer de mama ductal.

Figura de un tumor de mama ductal in situ (DCIS)

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

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Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

Figura de un tumor de mama invasivo

## Señales y síntomas

- Un bulto o hinchazón en la mama
- Cambios en el tamaño o la forma de la mama
- Cambios en la piel de la mama, como enrojecimiento o espesamiento de la piel
- Sangrado o flujo de líquido por el pezón
- Cambios en el pezón, como hinchazón, dolor o agrietamiento del pezón
- Dolor en la mama
- Cambios en la forma o el tamaño de la mama
- Cambios en la forma o el tamaño de la mama

## Causas del cáncer de mama

- Factores genéticos, como mutaciones en los genes BRCA1 y BRCA2
- Factores hormonales, como la exposición a hormonas durante largos períodos de tiempo
- Factores ambientales, como la exposición a radiación ionizante
- Factores de estilo de vida, como el consumo de alcohol y la obesidad
- Factores de edad, como el aumento de la edad
- Factores de raza, como el ser afroamericana
- Factores de antecedentes familiares de cáncer de mama
- Factores de antecedentes familiares de cáncer de mama

## Estadificación

La estadificación es el proceso de determinar el estadio del cáncer de mama. El estadio del cáncer de mama se determina en función de la extensión del tumor y si se ha extendido a los ganglios linfáticos y a otras partes del cuerpo.

Estadio I

El tumor mide 2 cm o menos

El tumor no se ha extendido a los ganglios linfáticos

El tumor no se ha extendido a otras partes del cuerpo

Estadio II

El tumor mide entre 2 y 5 cm

El tumor se ha extendido a los ganglios linfáticos

El tumor no se ha extendido a otras partes del cuerpo

Estadio III

El tumor mide más de 5 cm

El tumor se ha extendido a los ganglios linfáticos

El tumor se ha extendido a otras partes del cuerpo

Estadio IV

El tumor se ha extendido a otras partes del cuerpo

El tumor se ha extendido a los ganglios linfáticos

El tumor se ha extendido a otras partes del cuerpo

## Fibrocystic Breast Disease

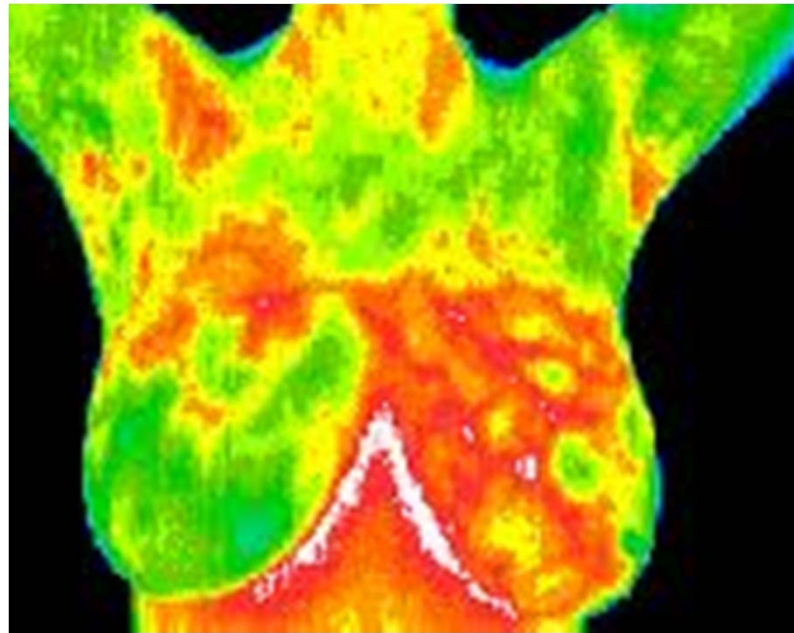
## Fibrocystic Breast Disease

axillary lymph nodes

fibrocystic changes  
mammary glands

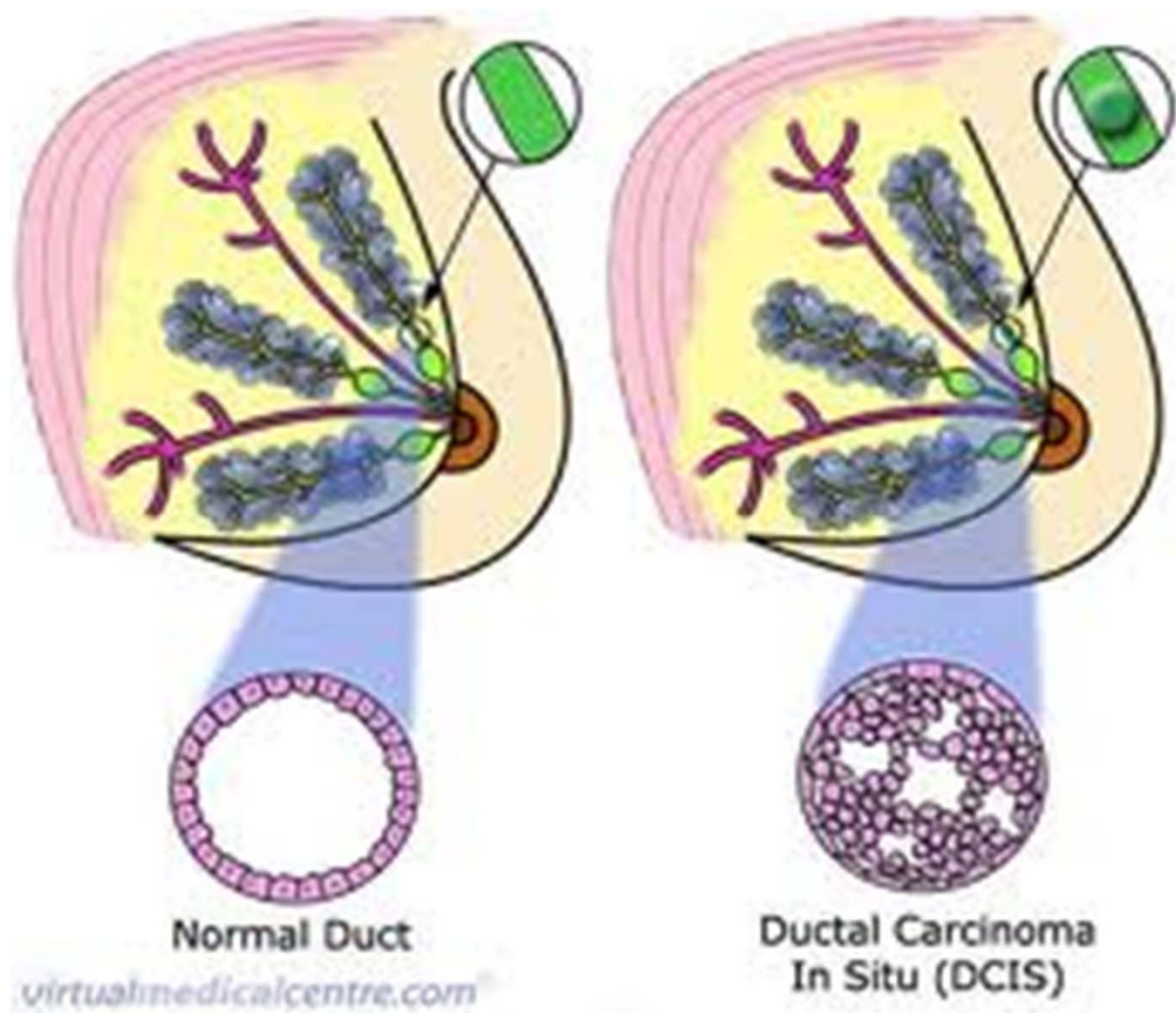
lactiferous ducts  
and nipple

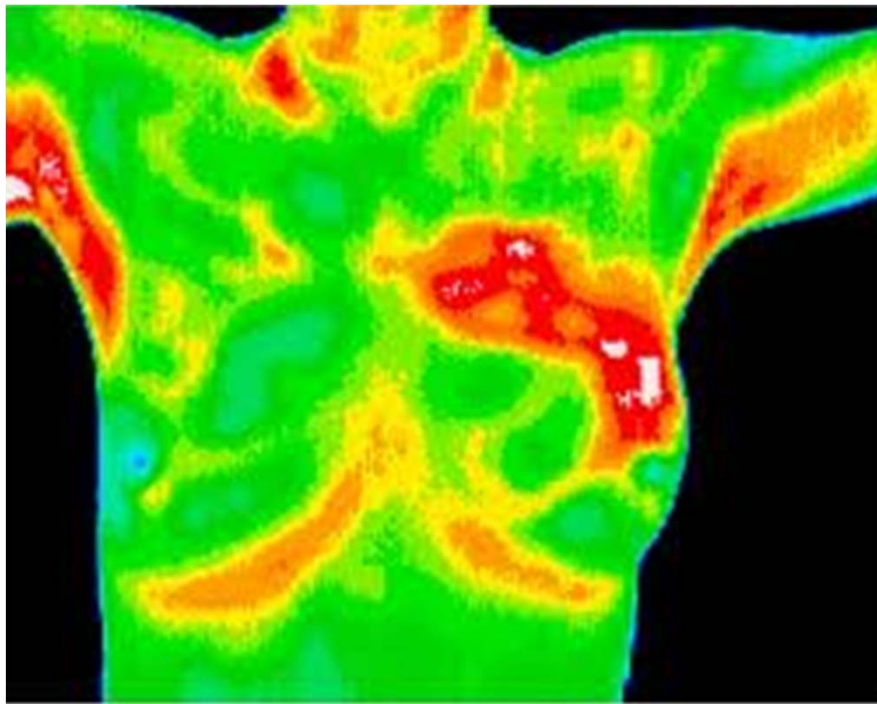
Anterior view of left breast and axilla



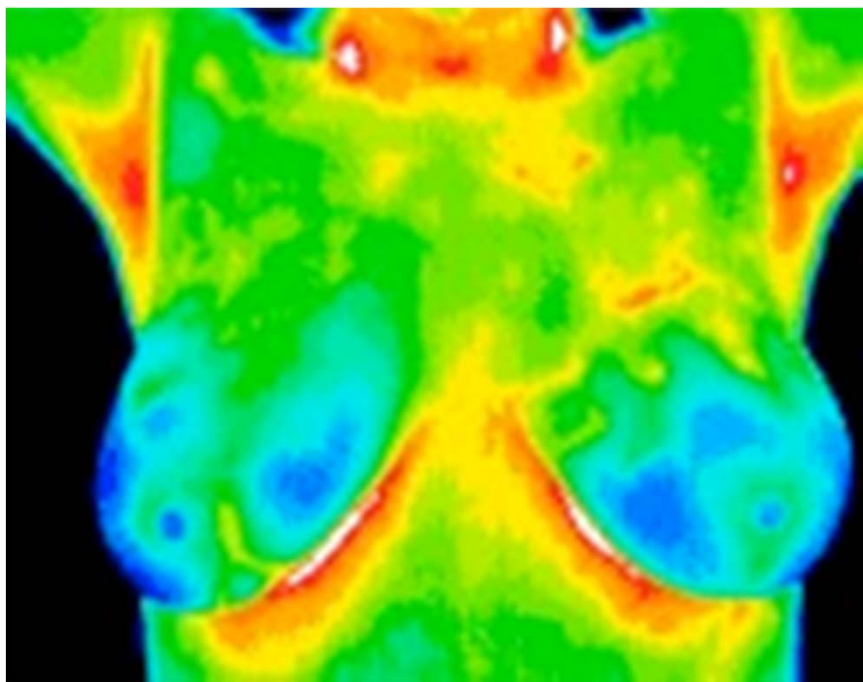
fibrocystic thermogram



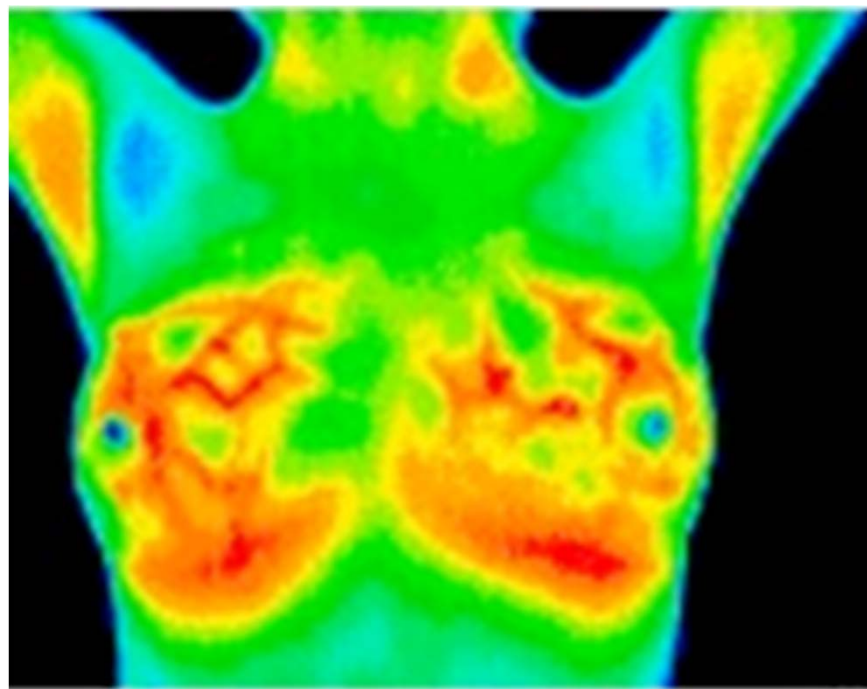




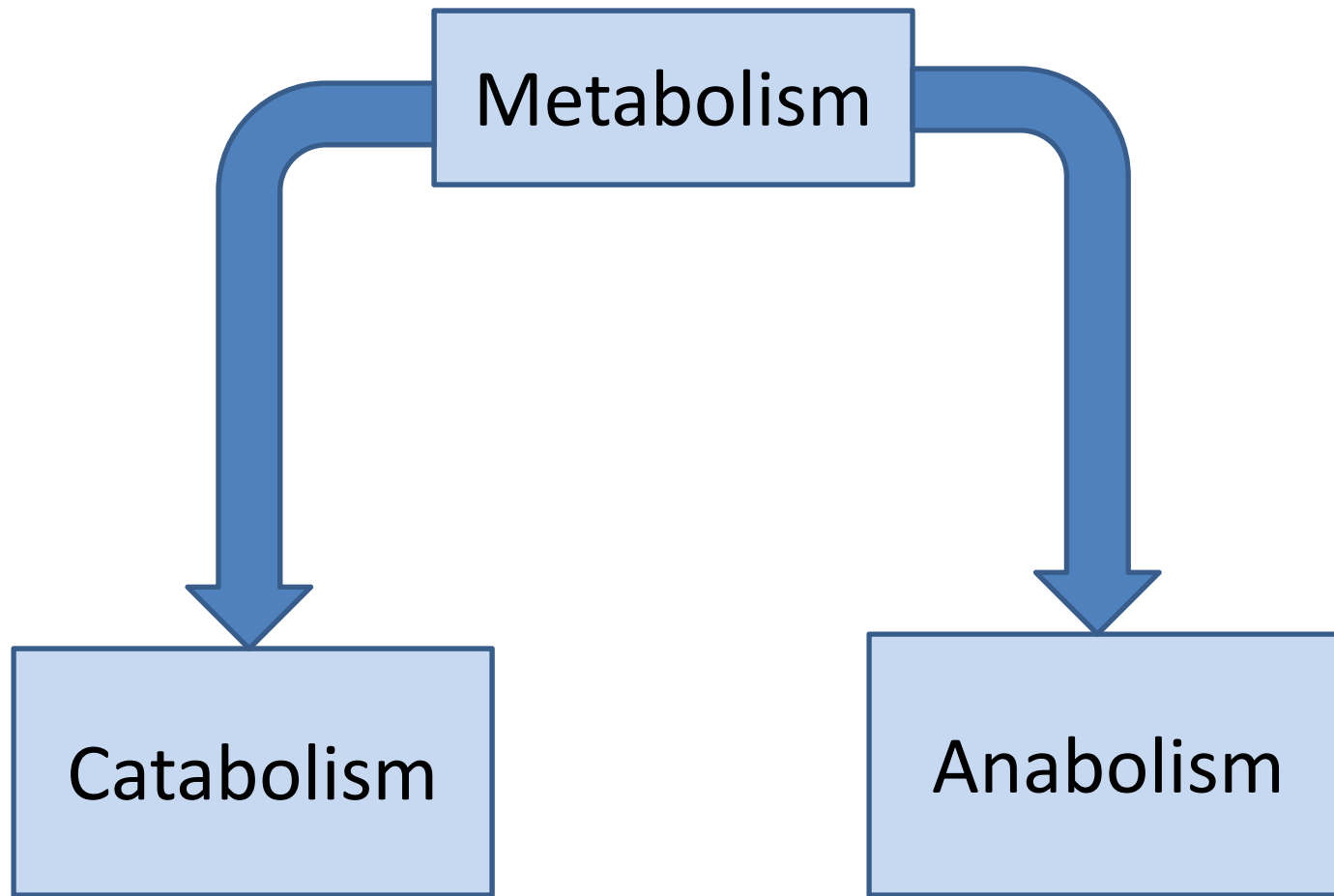
Ductal Carcinoma in Situ thermogram



normal

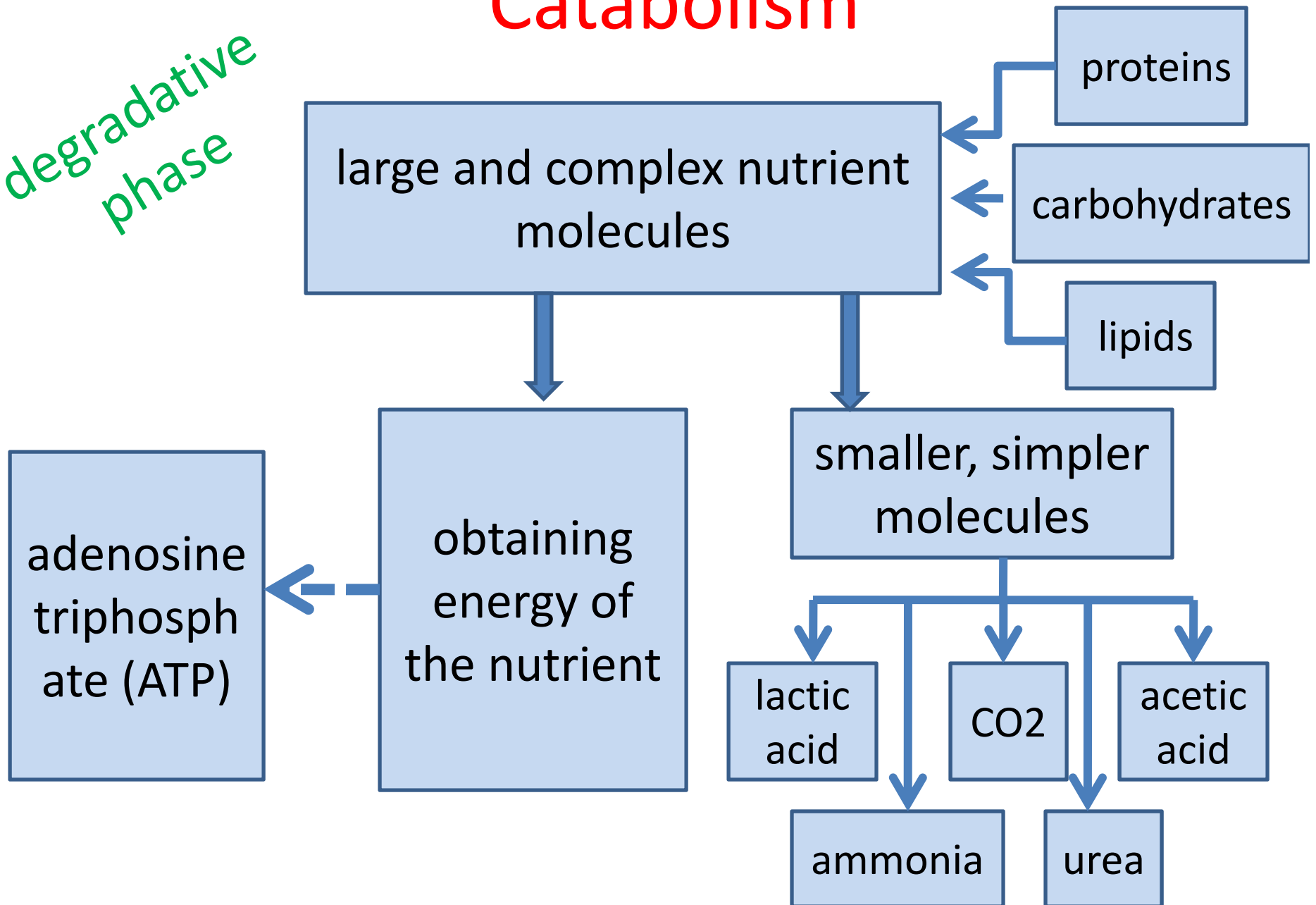


4 weeks pregnant



# Catabolism

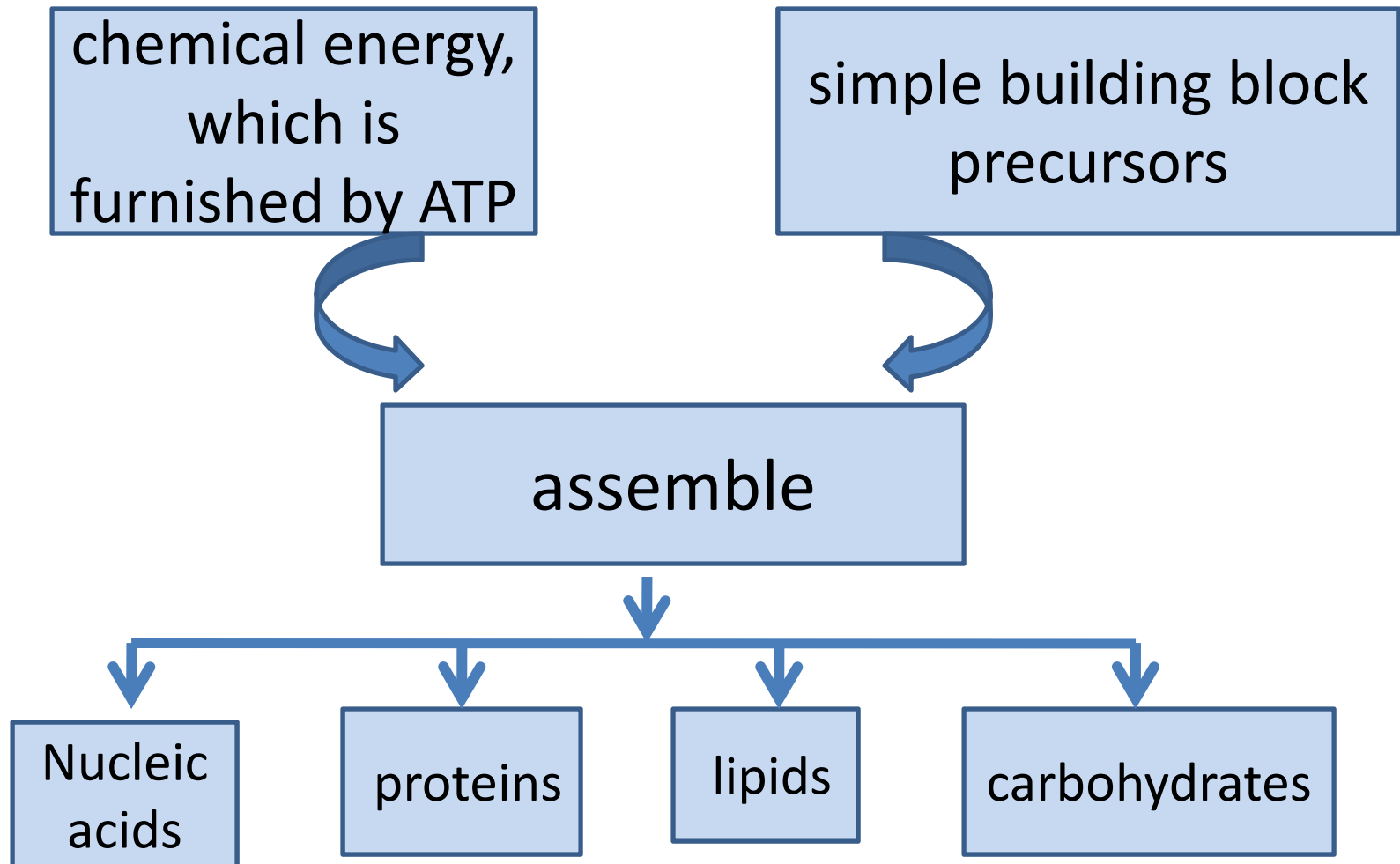
degradative  
phase





Building up  
phase

# Anabolism



# Normal cells

The energy  
produced

Is used  
by

cells for  
its division

a single cell

divides  
into

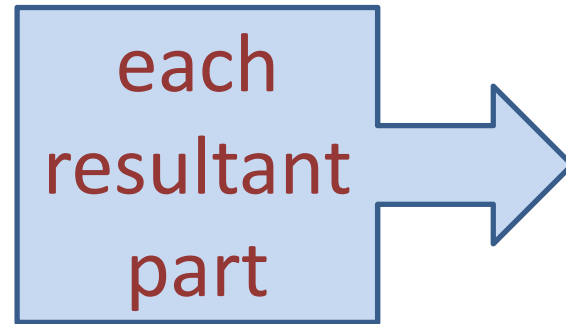
many cells and  
forms tissues

growth  
of

multicellular organs

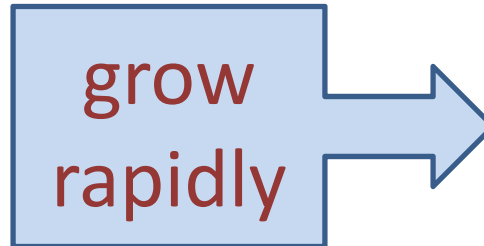
# Normal cells

In cell  
division



a complete relatively  
small cell

newly  
formed  
cells



reaching the size of  
the original cell

# Cancer cells

Lose



into organs

Cancer or

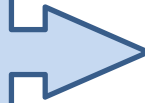
dividing undifferentiated  
mass of cells

Cancer cells do not obey  
normal pattern of tissue  
formation

have a distinctive type  
of metabolism

malignant cells

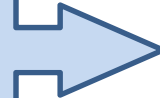
utilize



5 to 10 times  
as much glucose

convert most of it

into



Lactate instead of  
pyruvate

lactate

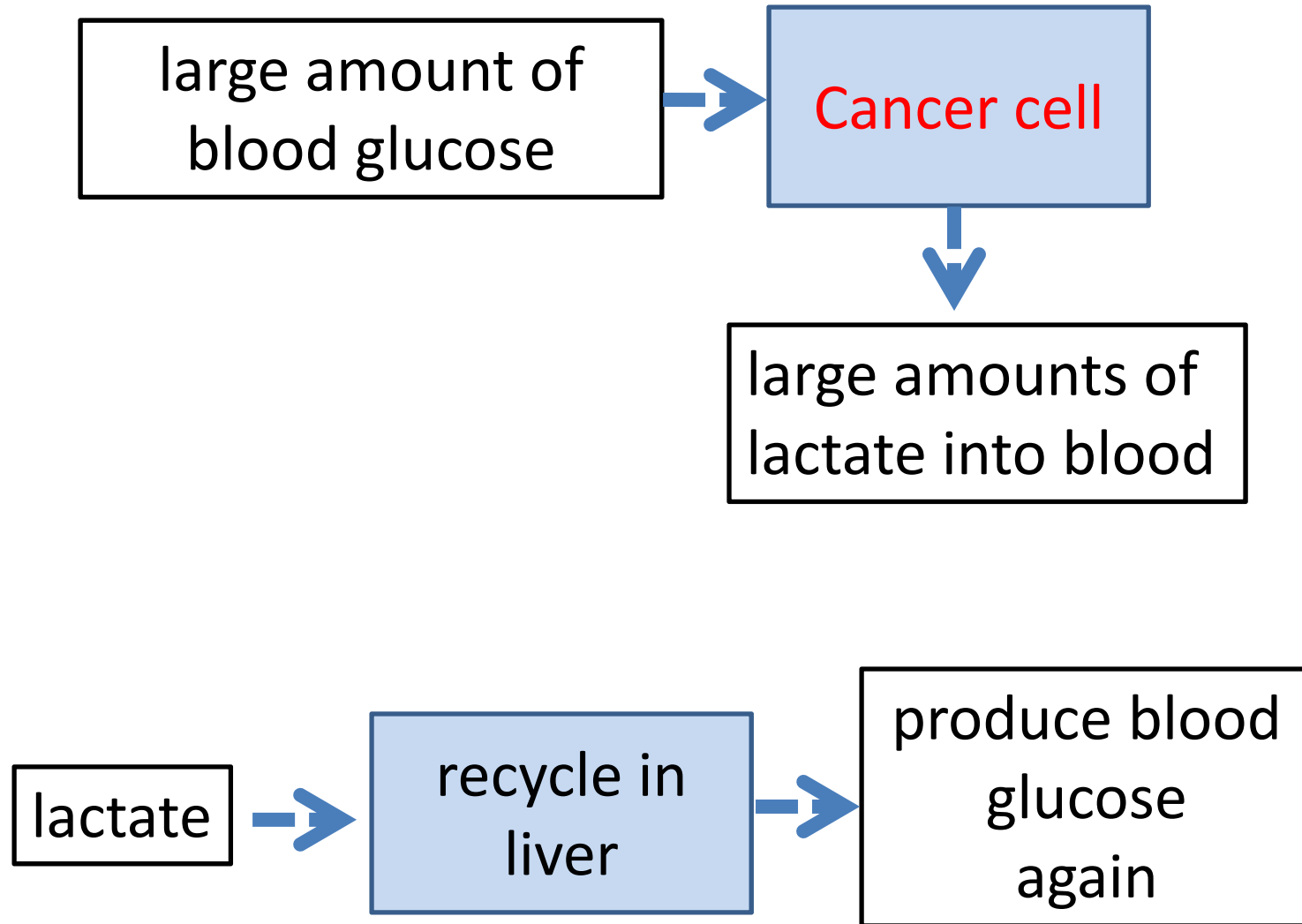


a low energy compound

pyruvate



a high energy compound



## glycolysis

glucose



lactate

produces 2 ATP molecules

lactate

In liver



glucose

requires 6 ATP molecules



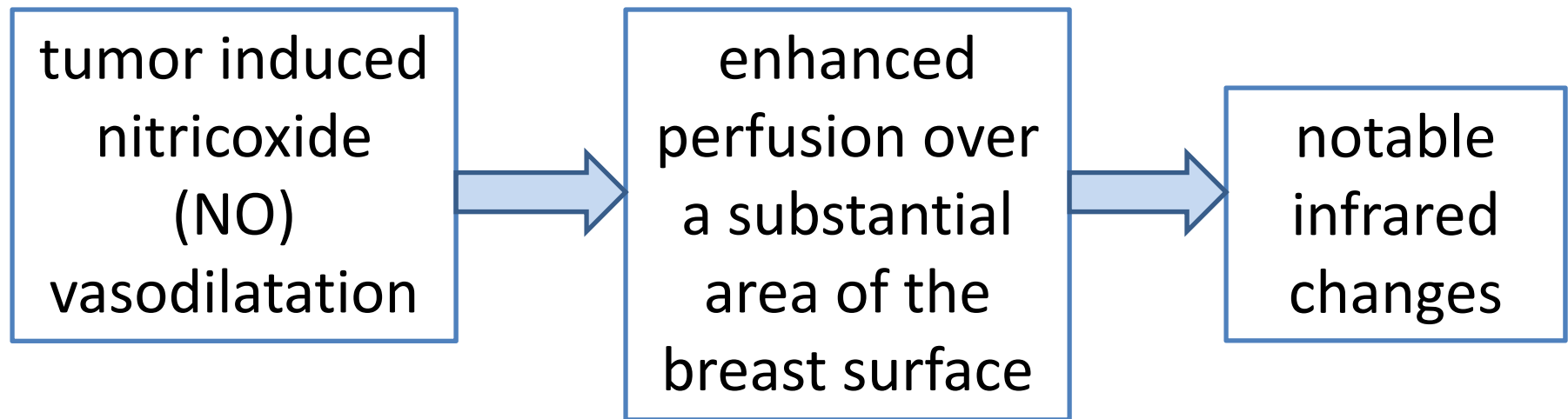
cancer cells

as metabolic parasites

dependent on the liver  
for a substantial part of their energy

High metabolic rate

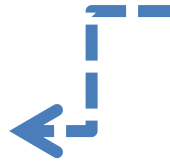
# Anbar



using tissue immunohistochemistry



nitric oxide  
**NO**

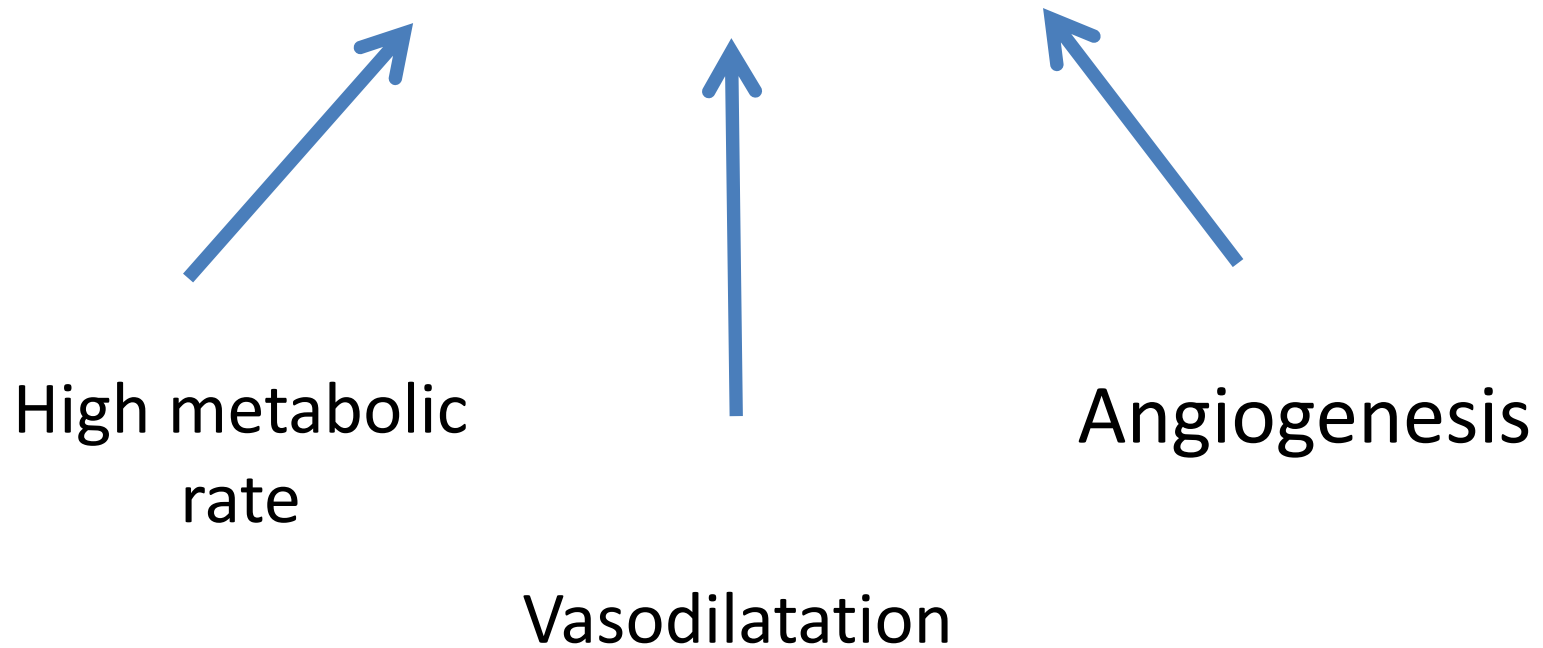


in breast carcinoma



high tumor grade

# Cancer cell hotter than normal cell



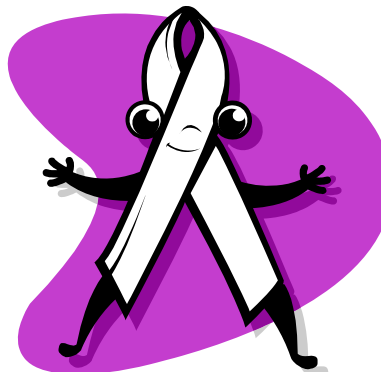
thermal IR imaging as a viable technique  
to visualize the abnormality

Advances in infrared (IR) camera technologies  
Ultra sensitive cameras

Fast computers

Advanced image processing  
techniques

Thermography for early breast cancer detection



In early 1980s

a standardized method of thermovascular analysis

20 discrete  
vascular and  
temperature  
attributes in  
the breast

+

pathologic prognostic features

tumor size

tumor grade

lymph node status

markers of tumor growth

standardized  
vascular patterning

temperatures across  
two breasts

Breast IR images  
(divide into 5 groups)

TH1  
normal  
uniform  
non-  
vascular

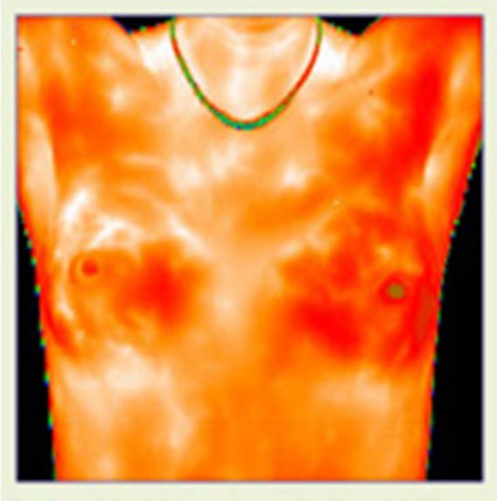
TH2  
normal  
uniform  
vascular

TH3  
Equi-  
vocal

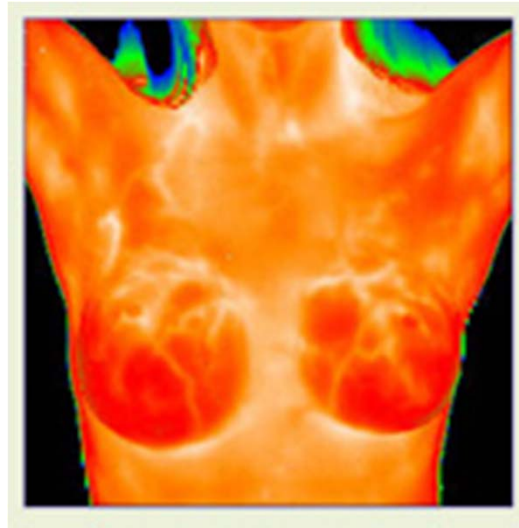
TH4  
abnormal

TH5  
severely  
abnormal

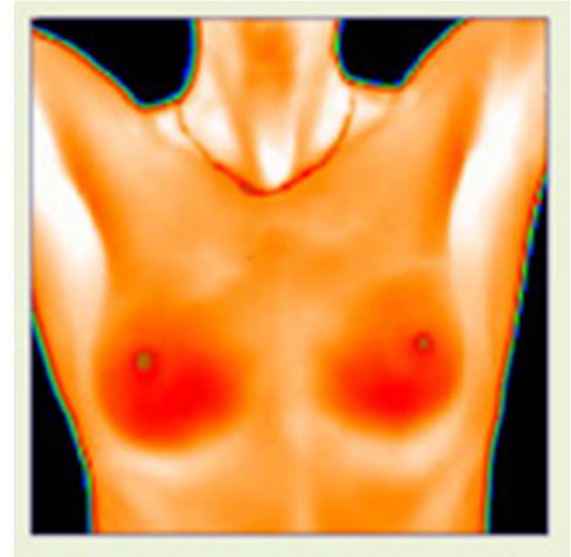
# Five different categories



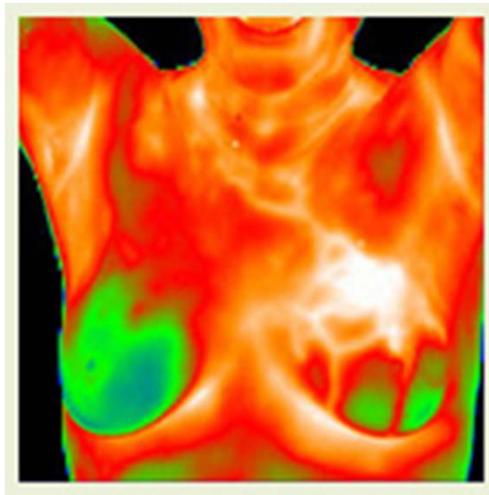
TH3



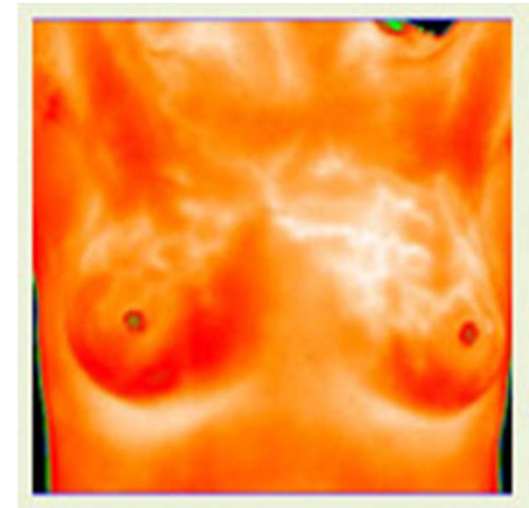
TH2



TH1



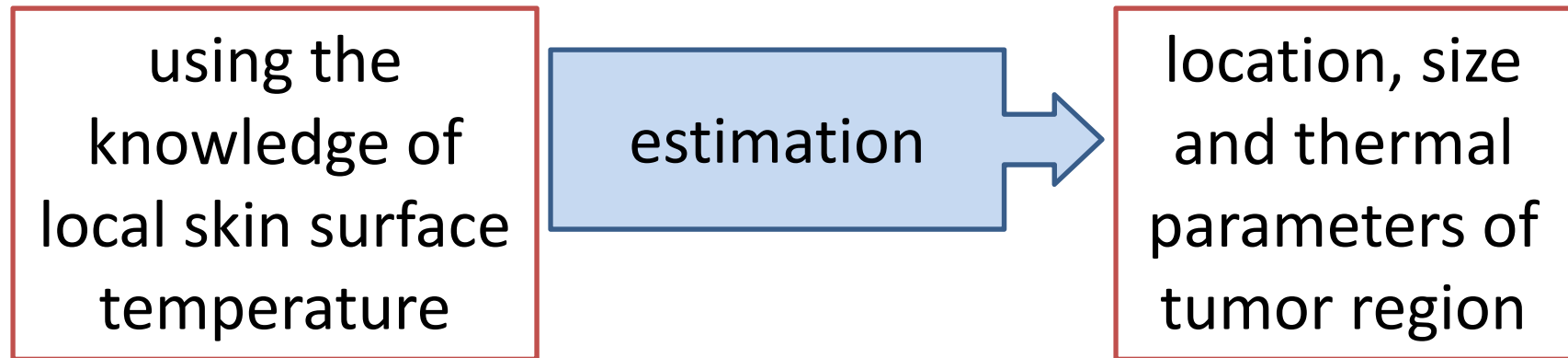
TH5



TH4



# inverse problem



# Pennes bio- heat equation

$$\frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) - C_b W_b (T - T_a) + q_m$$

study of heat transfer in biological systems

- $K$  the heat transfer by conduction through the tissue,
- $Q_m$  the volumetric blood perfusion rate whose magnitude was considered to be proportional to the arterial-venous temperature difference.
- $T_a$  temperature of arterial blood is approximated to the core temperature of the body and the venous blood approximated to the local tissue temperature
- $T$  temperature of tissue

# Numerical modelling of a female breast

(Ng and Sudharsan)

- The steady state Pennes bio-heat eq.

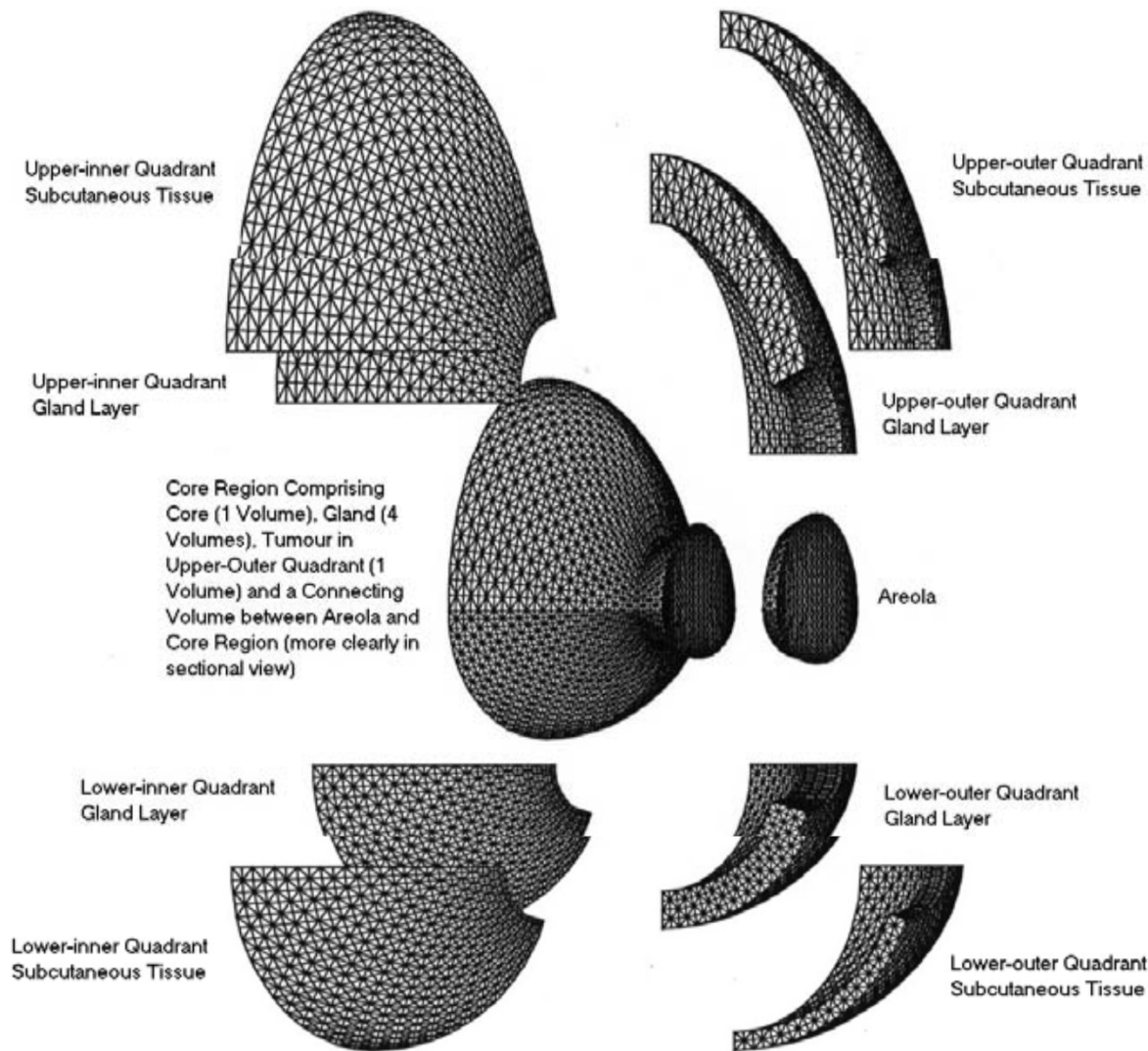
$$K\nabla^2 T - C_b W_b (T - T_a) + q_m = 0$$

- the boundary condition  $-K\nabla T = h(T - T_e)$
- $h$  is the overall heat transfer coefficient due to the combined effect of convection, radiation and evaporation.
- The bottom surface of the breast is the thoracic wall with core temperature of the body
- condition in this region is  $T = T_a$

# Numerical modelling of a female breast

(Ng and Sudharsan)

- The breast
- divided into four quadrants
- upper-outer quadrant (armpit), upper-inner quadrant
- lower-inner quadrant , lower-outer quadrant
- With various layers
- subcutaneous fat layer
- gland layer
- muscle layer
- unequal thickness
- using finite elements

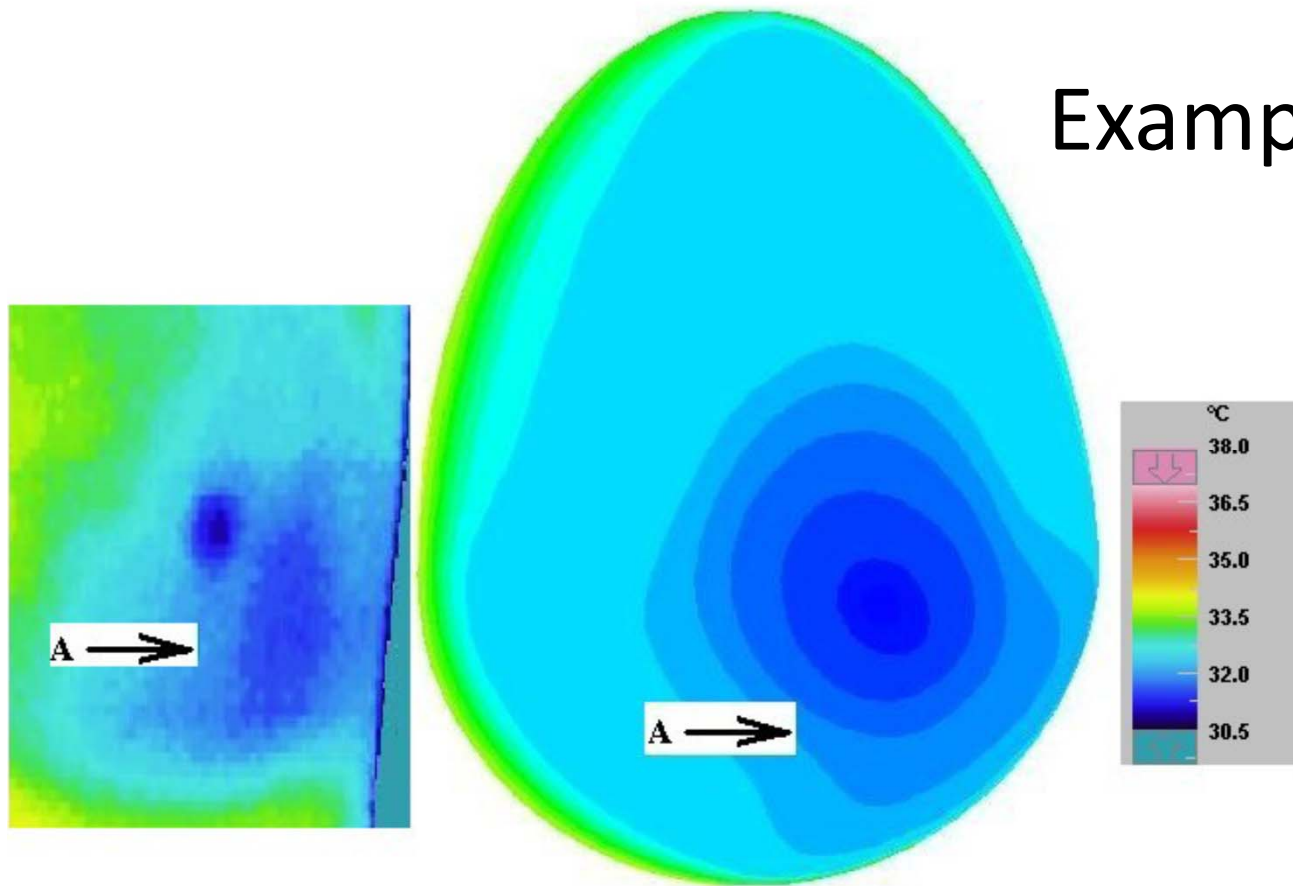


Exploded View of Various Tissue Volumes

E. Ng , N. M. Sudharsan , “Effect of blood flow, tumour and cold stress in a female breast : a novel time-accurate computer simulation” [Proceedings of the Institution of Mechanical Engineers, Part H: Journal of Engineering in Medicine, 215\(4\), pp. 393-404, 2001](#)



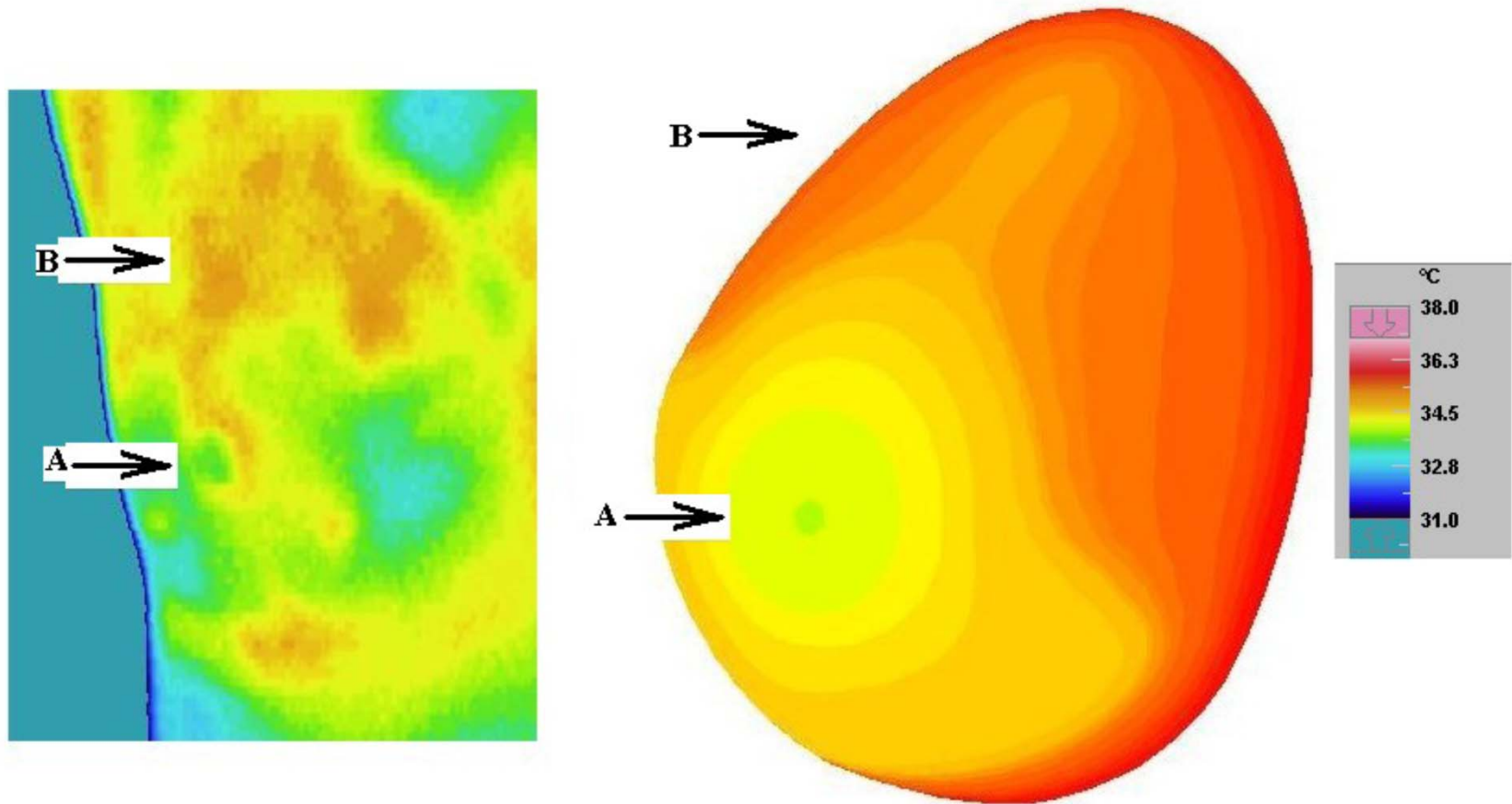
## Example 1



Normal Thermogram of a Left Breast with Numerical Simulation (Volunteer 1, Age 38 years)

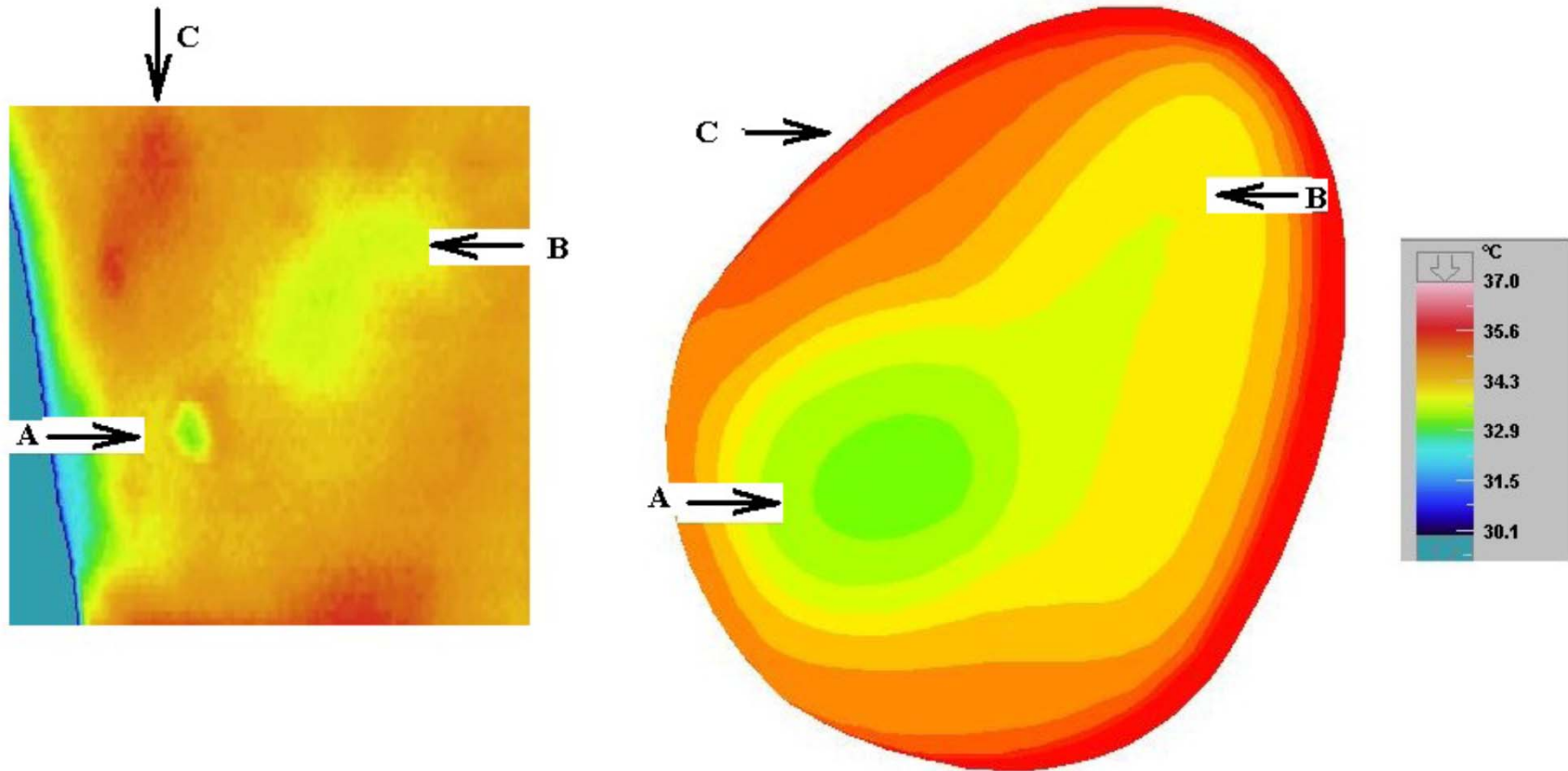
Ng , E., N M Sudharsan , Effect of blood flow, tumour and cold stress in a female breast: a novel time-accurate computer simulation [Proceedings of the Institution of Mechanical Engineers, Part H: Journal of Engineering in Medicine](#), 215(4), pp. 393-404, 2001

## Example 2



Abnormal Thermogram of a Right Breast with Numerical Simulation (Volunteer 2, Age 47 years)

# Example 3



Normal Thermogram of a Right Breast showing a cold area due to lumpectomy with Numerical Simulation (Volunteer 3, Age 43 years)

observation

numerical simulation

able to capture the presence of an abnormality

## Finite element thermal analysis (Lin et al. )

A 3D finite element thermal model of breast is built

- Exploring the relationship between an embedded small tumor and the resulting surface temperature distribution.
- Choosing a tetrahedron as the basic element

**Penn's bio-heat equation** under steady state conditions

$$\frac{\partial}{\partial x} (k_x \frac{\partial T}{\partial x}) + \frac{\partial}{\partial y} (k_y \frac{\partial T}{\partial y}) + \frac{\partial}{\partial z} (k_z \frac{\partial T}{\partial z}) + Q_m + \omega_b P_b C_b (T_a - T) = 0$$

•  $T$  and  $T_a$  temperature of tissue and arterial blood

$K_x$ ,  $K_y$  and  $K_z$  Thermal conductivity in x, y and z directions

$P_b$  and  $C_b$  density and specific heat of the blood

$K_x = K_y = K_z = K$  is assumed

$$K \frac{\partial T}{\partial S} \Big|_{Surface} = -h(T - T_e)$$

$h$  combined heat transfer coefficient due to convection, radiation and evaporation

$T_e$  surrounding temperature



# observation

- Early detection with
- a small tumor even in a deep region
- Environmental influences

# Thermal simulation of breast tumors

González

- bioheat Pennes equation

## observation

current state-of-the-art imagers are capable of

- detecting 3 cm tumors located deeper than 7 cm from the skin surface,
- tumors smaller than 0.5 cm can be detected if they are located close to the surface of the skin.

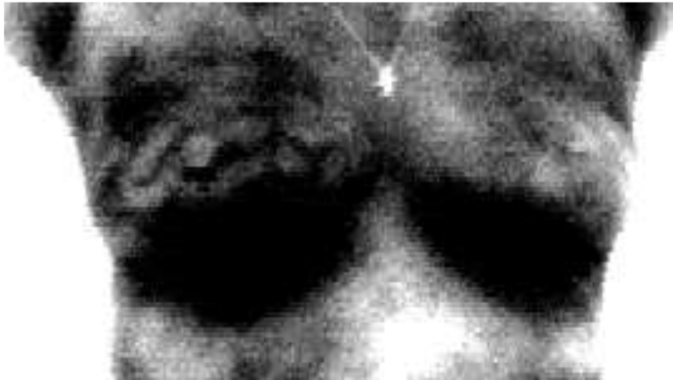
# Studies

1. Qi et al. (2 models)
2. Frize et al.
3. Wiecek et al.
4. Ng et al. (2 models)

# Automatic segmentation of two breasts (Qi et al.)

- Edge detection by canny edge detector
- Detection of 4 curves:  
left and right body boundary curves  
two lower boundaries of the breasts
- Using Hough transform to detect the lower boundaries
- Finally segmentation of left breast from right breast

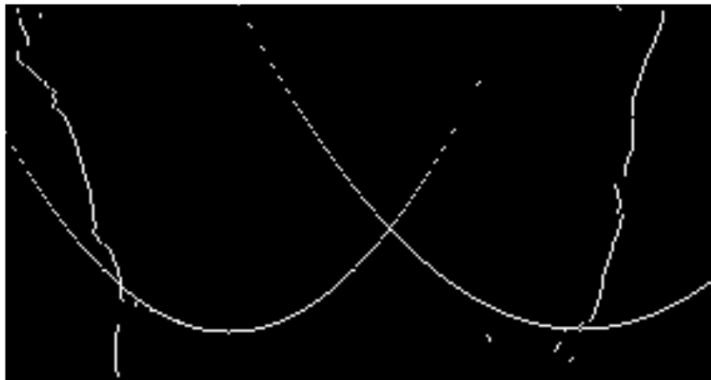
# Automatic segmentation of two breasts (Qi et al.)



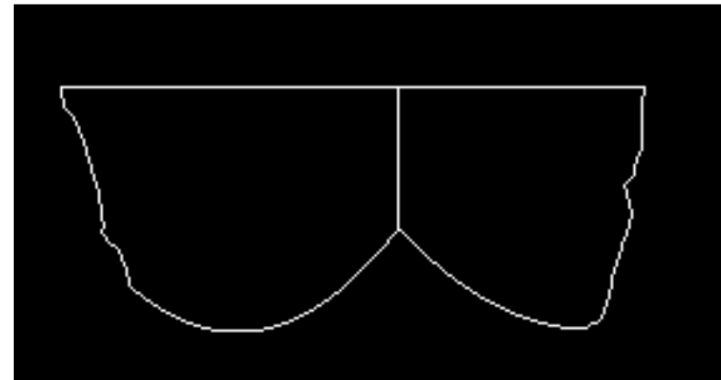
Original image



Edge detection by canny edge detector



Using Hough trans form to  
detect the lower boundaries



segmentation of left breast from  
right breast

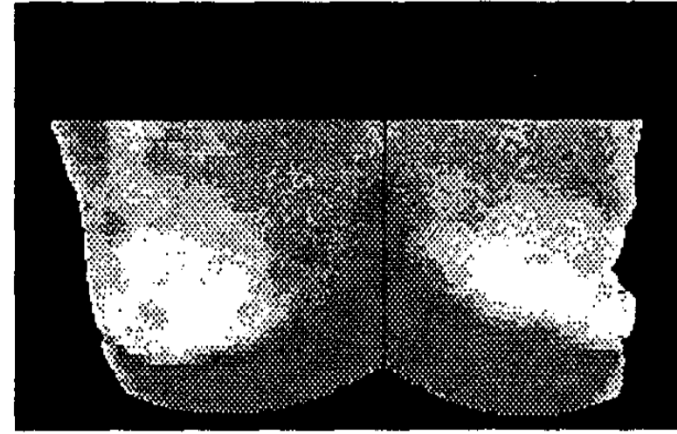
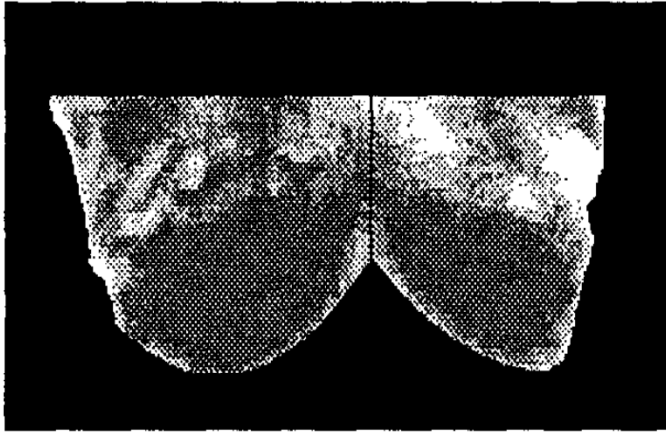
H. Qi, J. Head; "Asymmetry analysis using automatic segmentation and classification for breast cancer detection in thermograms", 2001

# Feature Extraction (Qi et al.)

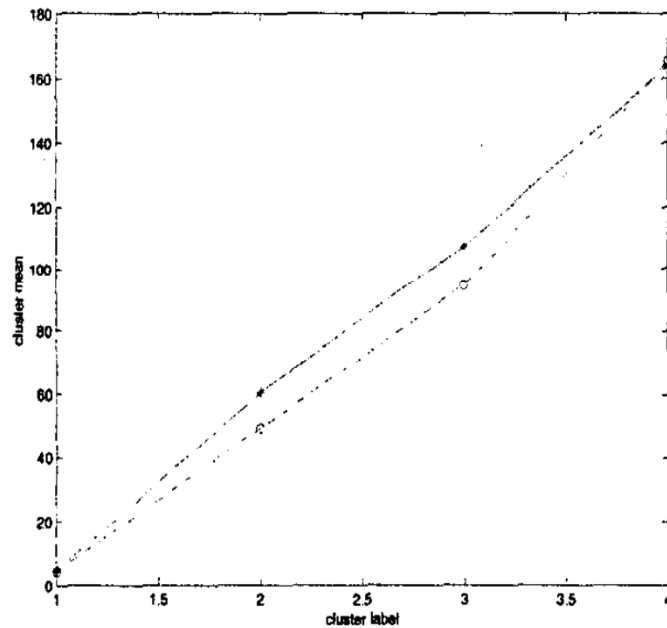
model	features	classifier
1	Means from 4 different regions and Left histogram and right histogram	K means
2	Means, variance, skewness, kurtosis, Entropy from each Breast Bilateral ratio close to 1= $\left  \frac{\text{feature value from left segment}}{\text{feature value from right segment}} - 1 \right $	Maximum Posterior Probability (MAP) KNN( <i>K-Nearest Neighbor</i>



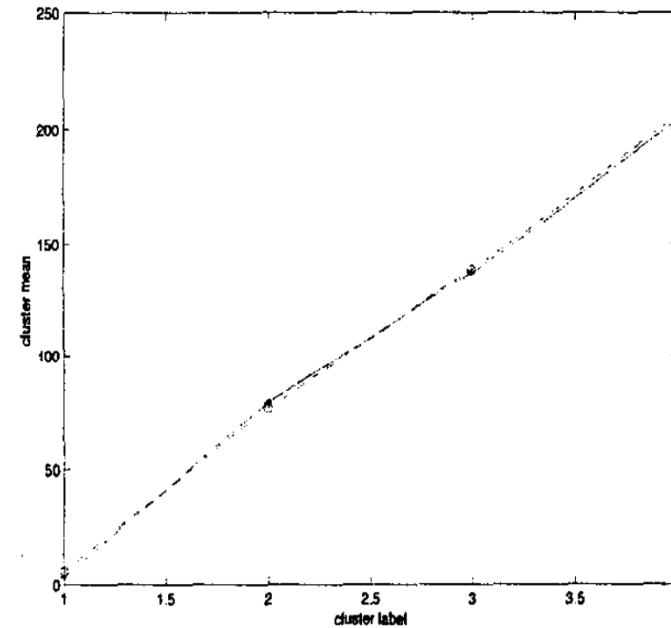
# Feature Extraction (Qi et al.)(model 1)



Means  
from 4  
different  
regions



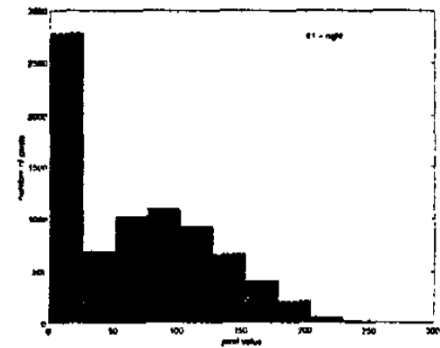
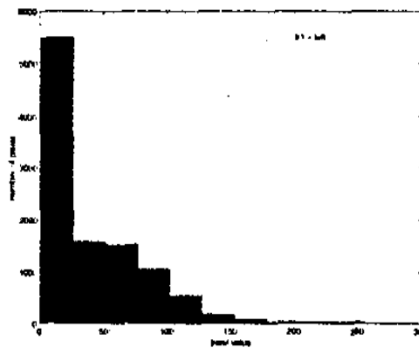
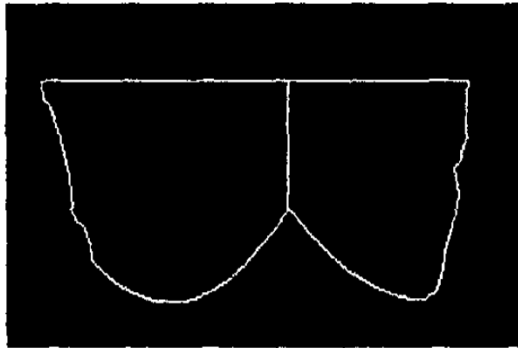
regions  
cancer



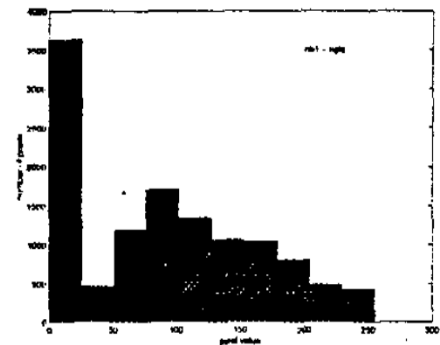
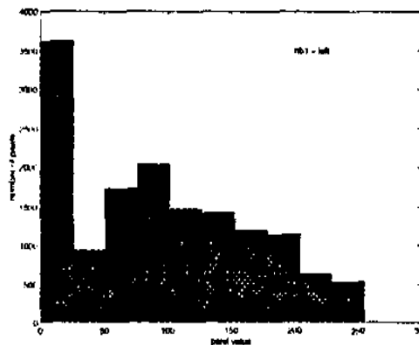
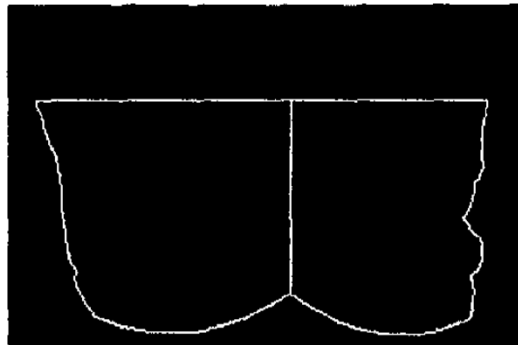
regions  
Non cancer

# Feature Extraction (Qi et al.)(model 1)

cancer



Non cancer

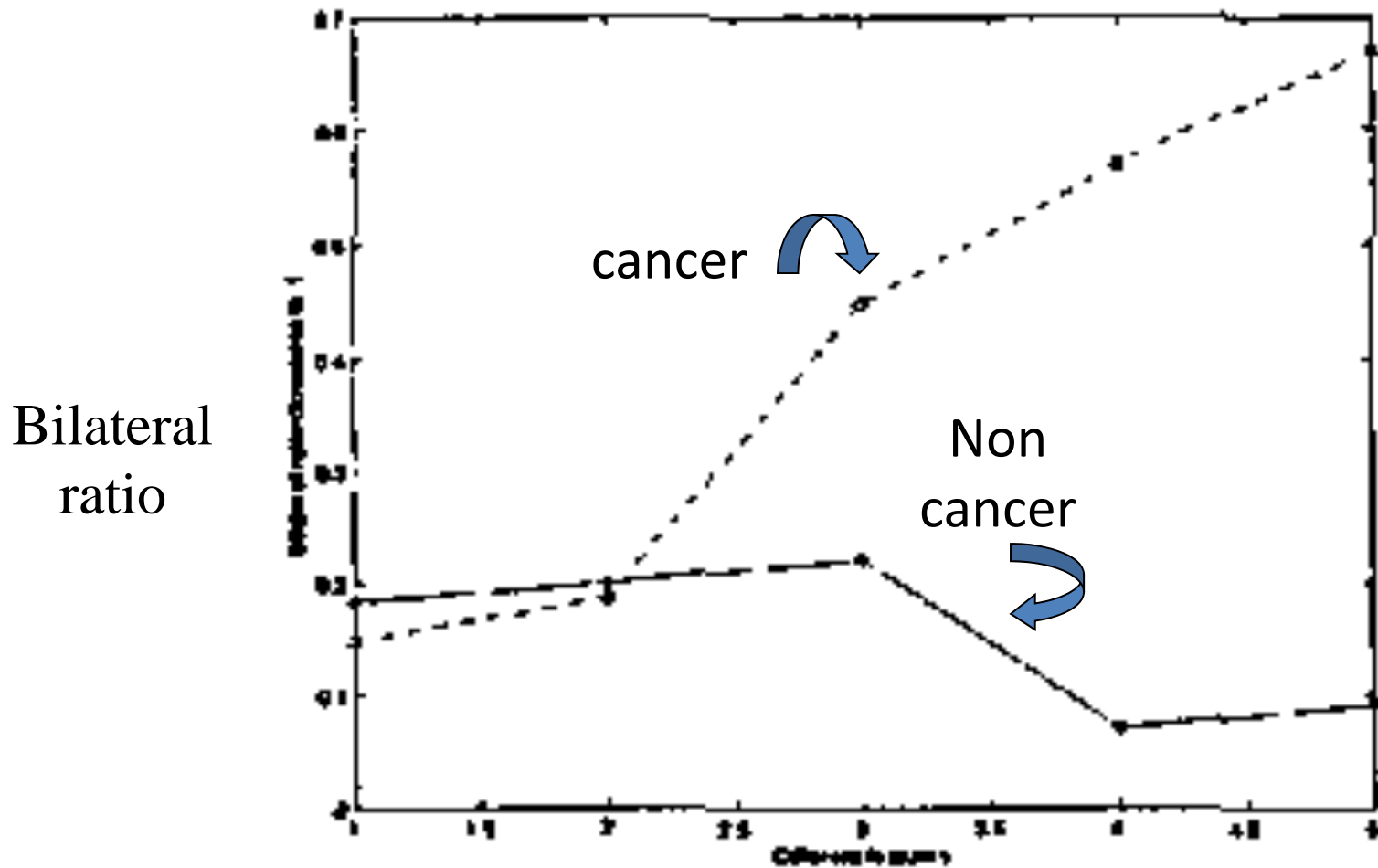


Right  
histogram

Left  
histogram

H. Qi, P. T. Kuruganti, " Detecting Breast Cancer from Thermal Infrared Images by Asymmetry Analysis"

## Feature Extraction (Qi et al.)(model 2)



# Automatic segmentation of two breasts (Frize et al.)

- morphological filtering operations :enhanced by using a disk of 5-pixel radius to perform top-hat and bottom-hat
- The circular nature of each contour fitting by an ellipse
- The ellipse-fitting algorithm by Halir and Flusser's algorithm
- each breast divides to four quadrants by nipple and chin

# Automatic segmentation of two breasts

(Frize et al.)



N. Scales, C. Herry, M. Frize, " Automated Image Segmentation for Breast Analysis Using Infrared Images", 2004

## Frize et al.

features	classifier
<p>for each breast and each quadrant within the breasts:</p> <p>mean, standard deviation, median, maximum, minimum, skewness, kurtosis, entropy, area and heat content</p>	<p>Neural Network back propagation</p>

## Wiecek et al.

features	classifier
<p><b>First order statistical parameters (Histogram based)</b> mean value , variance skewness, kurtosis, energy and entropy</p> <p><b>Second order statistical parameters (co occurrence matrix based)</b> Energy,Variance, Difference variance,Correlation, Inverse difference, Entropy</p>	<p><i>Artificial Neural Network (ANN)</i></p>



# Feature Extraction (Ng et al.)

model	features	classifier
1	<ul style="list-style-type: none"><li>•File FH: <b>Biodata</b>: patient age, family history, hormone replacement therapy, age of menarche, presence of palpable lump, previous surgery/biopsy, presence of nipple discharge, breast pain, menopause at age above 50 years, and first child at age above 30 years.</li><li>•File T: mean, median, modal, standard deviation and skewness of temperature for left and right breasts.</li><li>•File TH: combination of FH and T.</li><li>•File TD: temperature difference of mean, median, modal, standard deviation and skewness for left and right breasts.</li><li>•File TDH: combination of TD and FH.</li></ul>	(complementary learning fuzzy neural network) FALCON-AART

# Feature Extraction (Ng et al.)

model	features	classifier
2	<ul style="list-style-type: none"><li>•File FH: Bio-data from questionnaire</li><li>•Temperature data from thermograms<ol style="list-style-type: none"><li>1. Mean temperature of left breast</li><li>2. Mean temperature of right breast</li><li>3. Median temperature of left breast</li><li>4. Median temperature of right breast</li><li>5. Modal temperature of left breast</li><li>6. Modal temperature of right breast</li></ol></li></ul>	<i>Artificial Neural Network (ANN)</i> Radial Basis Function Network (RBFN)

# fractal

A fractal is a non-regular geometric shape that can be split into parts which possess self similarity. In another words, it has same degree of irregularity on all scales

# **a very intuitive access to the language of fractal geometry**

- consider a copy machine with an image reduction feature
- After some ten or so cycles any initial image would be reduced to just a point.



# A fractal has several characteristic

- fractal scaling. The same level of detail occurs at all scales within the fractal so that as one delves deeper into the fractal, it never simplifies.

## A fractal often has the following features:

- It has a fine structure at arbitrarily small scales.
- It is too irregular to be easily described in traditional Euclidean geometric language.
- It is self similar.
- It has a Hausdorff dimension which is greater than its topological dimension.
- It has a simple and recursive definition.

- self-similarity. The shapes seen at one scale of a fractal closely resemble the shapes seen at all other levels of detail.

No matter how many times a certain area of the fractal is magnified, self-similarity will be Maintained

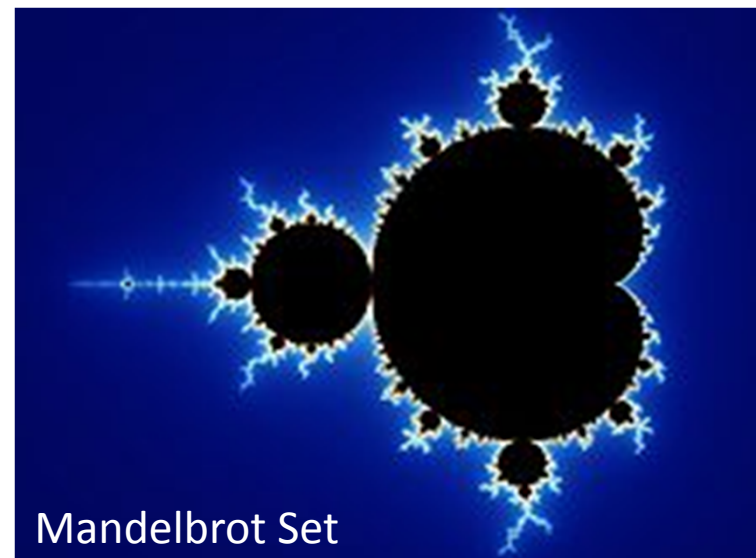
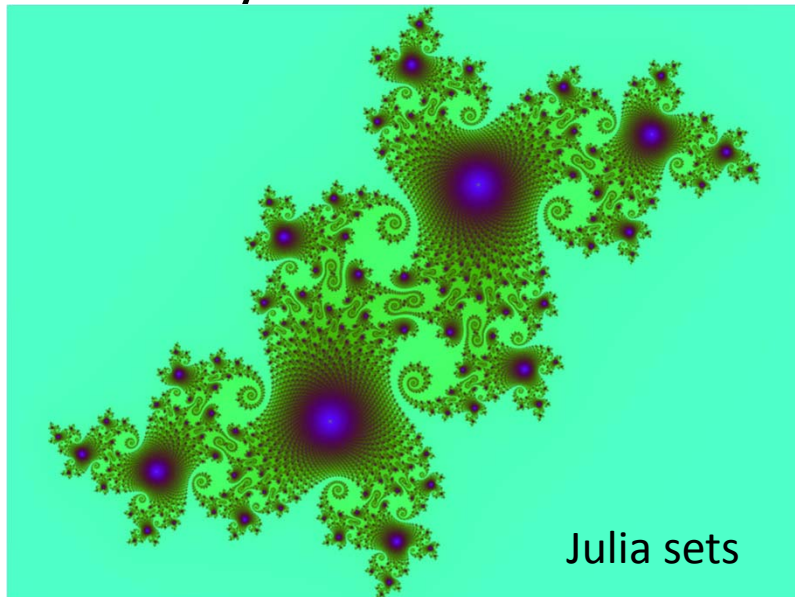
- geometry between dimensions, which means that a fractal exists in any one of an infinite number of dimensions (Brigs 20).

Imagine a string, twisted in a self-similar pattern into the shape of a square. Does the string exist as a one-dimensional line, or did it develop into a two dimensional plane?

(Brigs 65). Mandlebrot's fractal dimension for this figure is somewhere around 1.26, neither one dimensional nor two.



The father of fractals is often considered to be a man by the name of Gaston Julia. In the early 1900's, Julia did much research on iterated functions, and even drew some of his famous Julia sets by hand. True, there were some other works out there, such as Sierpinski's triangle and Koch's curve, but Julia's work was a major breakthrough. Until the 1960's much of the work with fractals was abandoned due to lack of technology. That changed in the 1970's when Mandelbrot used computers to create what we now know today as the Mandelbrot Set.



# **Mandelbrot is largely responsible for the present interest in Fractal Geometry**

- He showed how Fractals can occur in many different places in both Mathematics and elsewhere in Nature.

# The most common dimensions in fractal analysis

- Hausdorff dimension
- Self similarity dimension
- Fractal dimension

# Hausdorff dimension

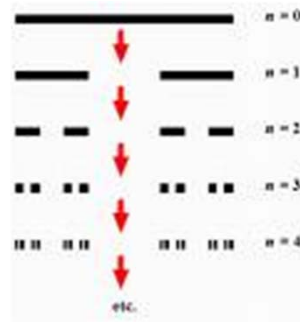
- Fractal is an object whose Hausdorff dimension is greater than its topological dimension.
- the Hausdorff dimension of a single point is zero, of a line is one, of the plane is two.
- many irregular sets(fractals) that have non integer Hausdorff dimension

# Fractal Dimension(FD)

- Fractal Dimension is a statistical quantity
- indicates how completely a fractal would fill the space in different scales or magnification

# A class of examples (for generating fractals)

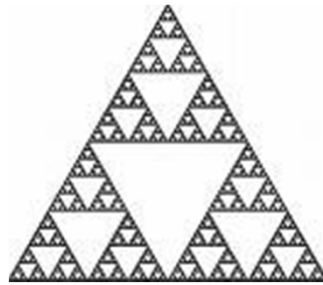
- Cantor set



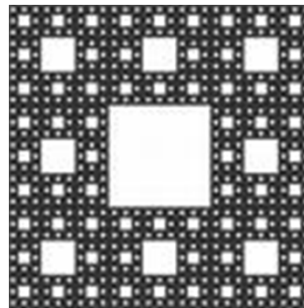
- Menger sponge



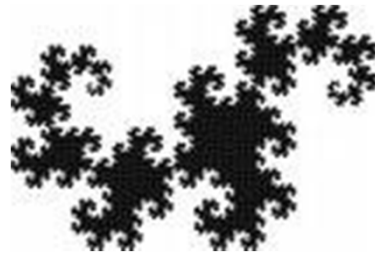
- Sierpinski triangle



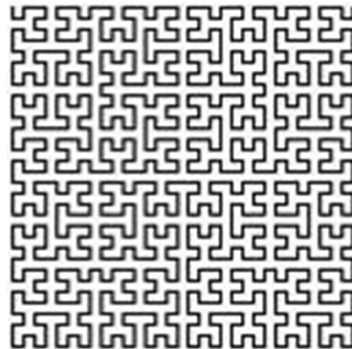
- Sierpinski carpet



- Dragon curve

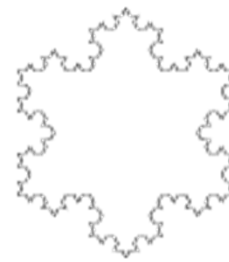


- Space filling curve



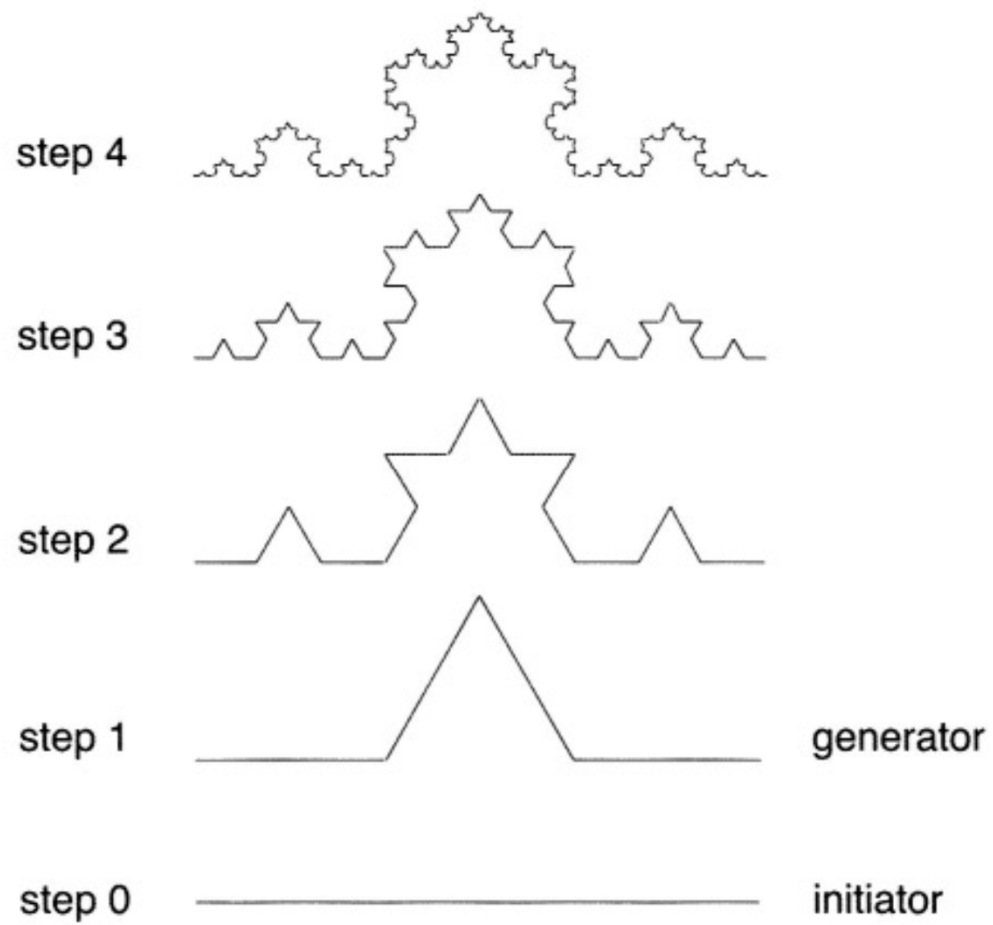


- Koch curve



## Example (How to compute FD of Koch Snowflake)

- At zeroth level ( $n=0$ ) the step size is 1
- At the next level ( $n=1$ ), the step size is  $1/3$
- And so on



$$N_s = 4^n, L_s = 3^{-n} \Rightarrow n = -\frac{\log L_s}{\log 3} \Rightarrow N_s = 4^{-\log L_s / \log 3} \Rightarrow \log N_s = \frac{\log 4}{\log 3} \log L_s.$$

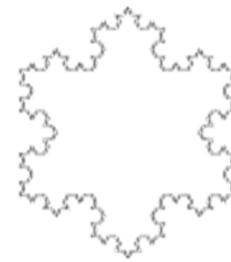
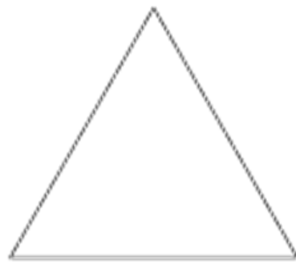
$$\frac{\log N_s}{\log L_s} = \frac{\log 4}{\log 3}$$

FD=  $\log 4 / \log 3$  which is approximately  
1.26.



# Example (How to create Snowflake)

- is built by starting with an [equilateral triangle](#),
- removing the inner third of each side,
- building another [equilateral triangle](#) at the location where the side was removed,
- repeating the process indefinitely.



## Examples of some fractals by their Hausdorff dimension

- Cantor set 0.6309
- Koch curve 1.2619
- Dragon curve boundary 1.5236
- Sierpinski triangle 1.585
- Sierpinski carpet 1.8928
- Menger sponge 2.7268

# how to calculate fractal dimension?

- The simplest way to calculate FD is by taking the advantage of self-similarity
- Suppose we have a one dimensional line segment. If we look at it with the magnification of two, we will see two identical line segments, and  $2^1 = 2$ , where 1 indicates the dimension. In a two dimensional square, with the magnification of 2, we get 4 identical shapes in both of them and  $2^2 = 4$  and hence 2 indicates the fractal dimension. Finally, take a three-dimensional cube and doubling its length, breadth and height, we get eight identical cubes, that is  $2^3 = 8$  and 3 indicates the fractal dimension.

This can be expressed as

$$E^D = N$$

Here, E stands for the magnification, D for dimension and N for the number of identical shapes. Applying logarithms,

$$D = \log N / \log E$$



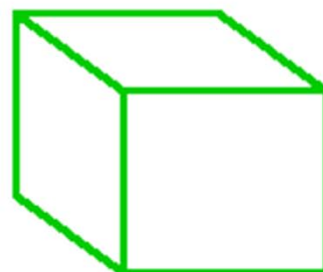
$$D = 1$$



$$D = 2$$



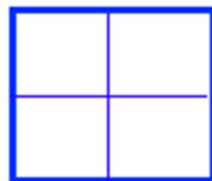
$$D = 3$$



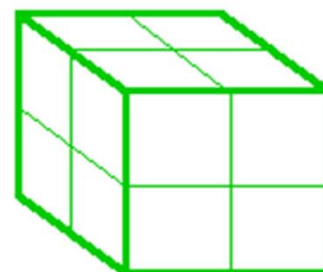
$$r = 2$$



$$N = 2$$



$$N = 4$$

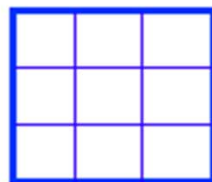


$$N = 8$$

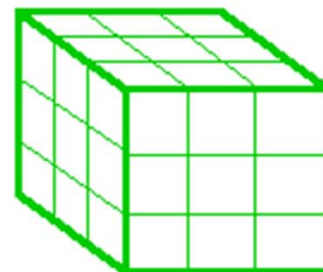
$$r = 3$$



$$N = 3$$



$$N = 9$$



$$N = 27$$

$$N = r^D$$

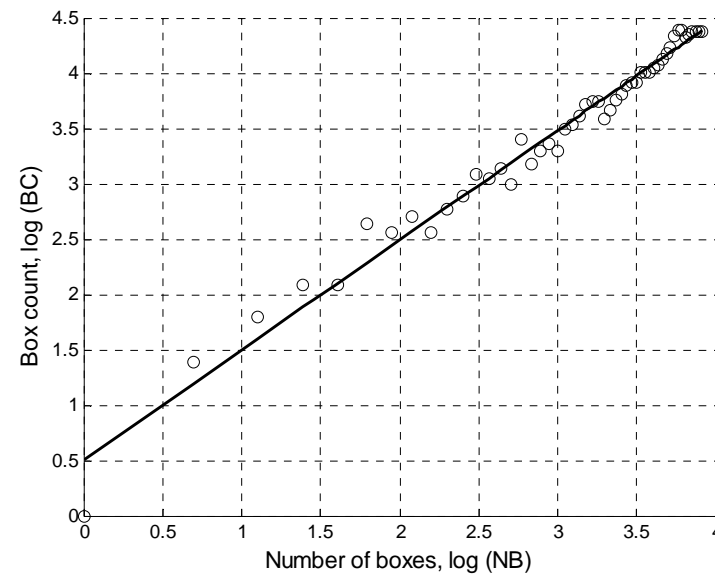
# self similarity dimension

$$a \propto \frac{1}{S^D}$$

- $D$  is the self similarity dimension
- $a$  is the number of self similar pieces at reduction factor  $(1/S)$ , so

$$D = \frac{\log(a)}{\log(\frac{1}{S})}$$

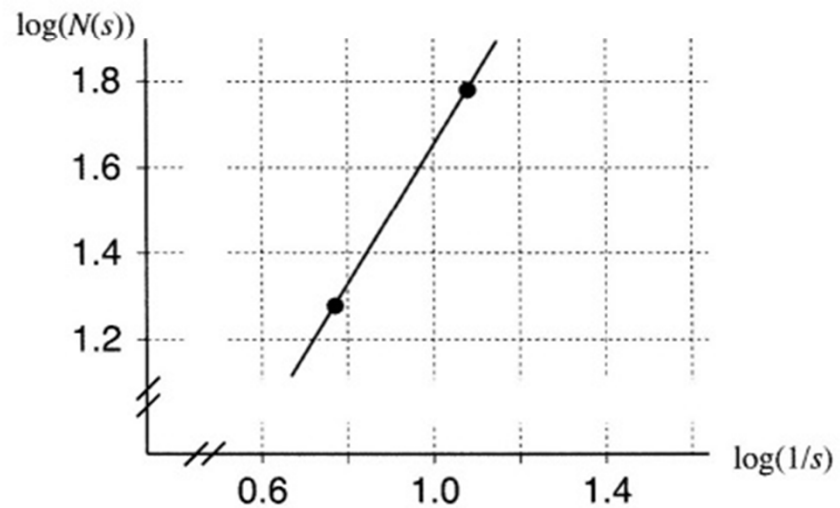
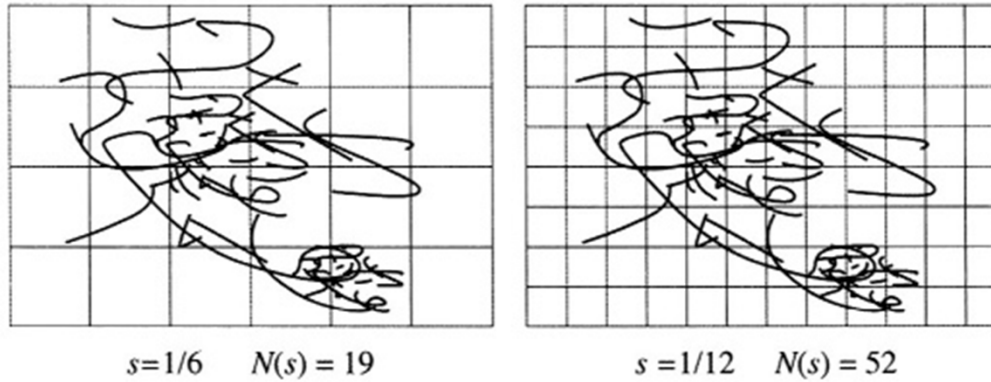
- D can be estimated by slope of the straight line approximation for a plot of  $\log(a)$  vs.  $\log(1/s)$ .



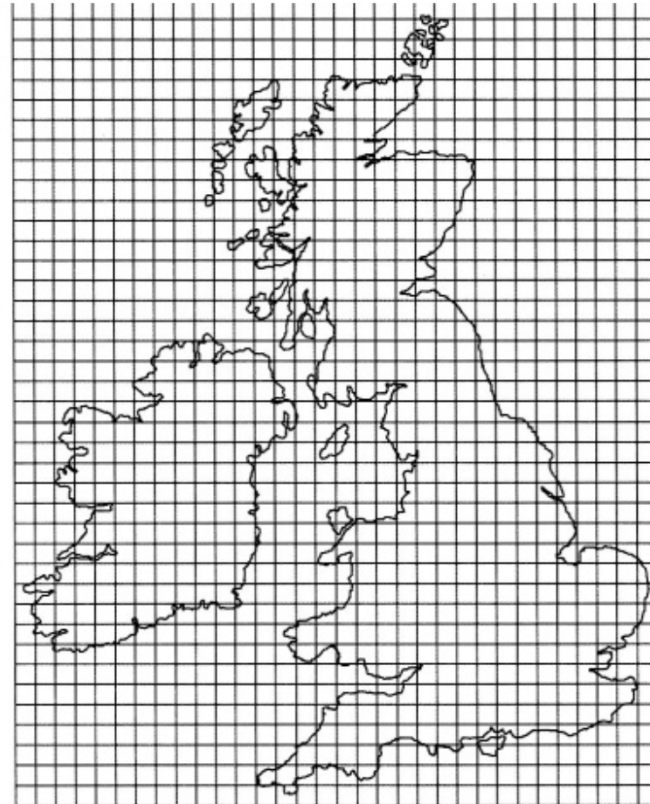
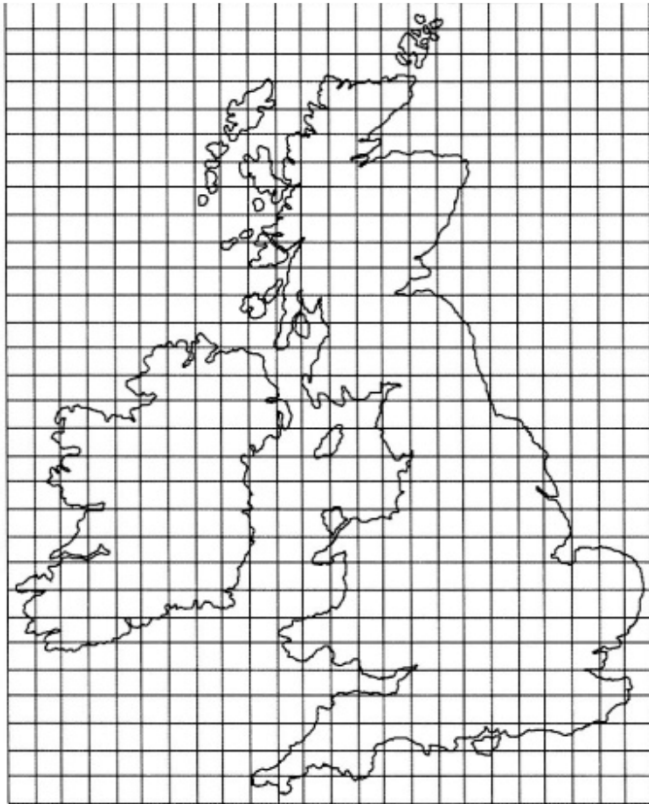
# Box counting method (BCM)

- partitioning the image into square boxes with equal sizes and
- then counting the number of boxes which contain a part of the image.
- repeating the process with partitioning the images into smaller and smaller size of boxes.
- The plot of  $\log$  of the number of boxes counted vs. the  $\log$  of the magnification index for each stage of partitioning
- The slope of best fitting line to the aforementioned plot is the FD of pattern.

# Example 1(BCM)



## Example 2(BCM) (Coastline of Britain)

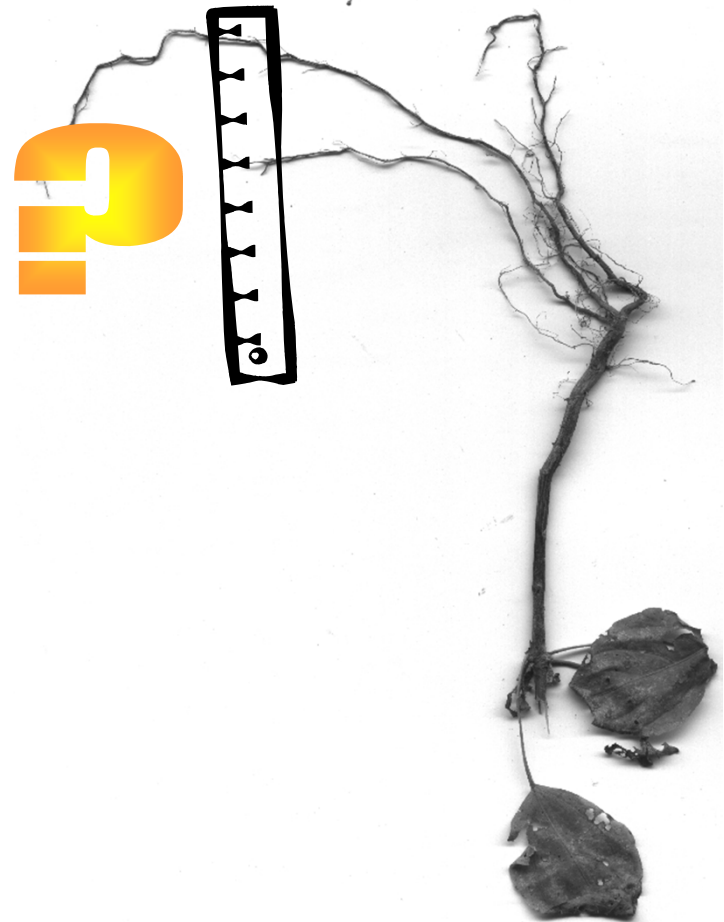


$$d = \frac{\log 283 - \log 194}{\log 32 - \log 24}$$

which is approximately 1.31

# A FRACTAL IS A SHAPE THAT CAN'T BE DESCRIBED BY THE USUAL GEOMETRIC TERMS

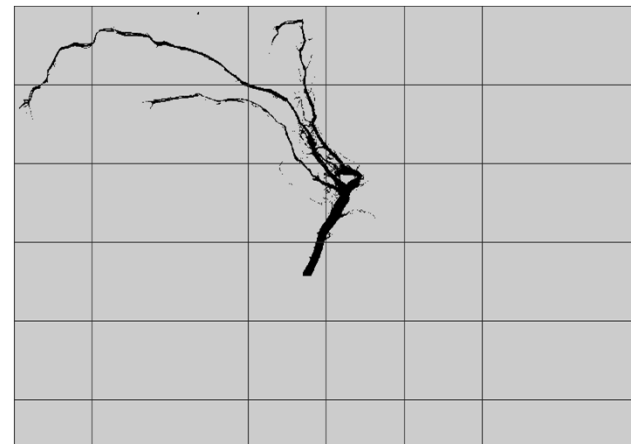
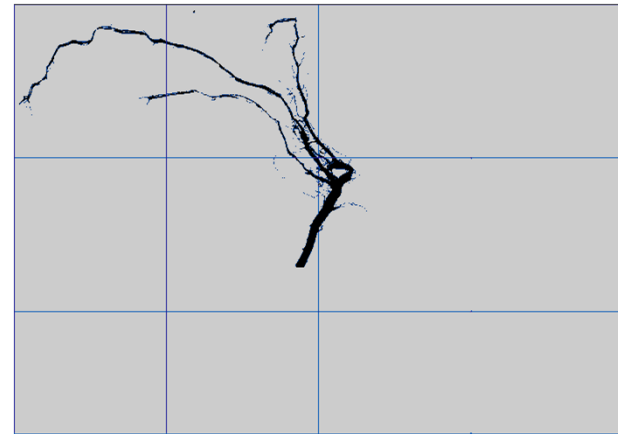
- For example, what shape is a plant's root?
- More importantly, how do you measure a plant's root?





# FRACTALS AREN'T MEASURED BY CONVENTIONAL METHODS

- We can use something called a “box count”
- We count how many squares in grids of different sizes the fractal occupies.
- As the grid gets smaller, the number of squares occupied gets bigger exponentially!



# Ten different contours



(1)



(2)



(3)



(4)



(5)



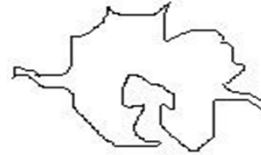
(6)



(7)



(8)



(9)

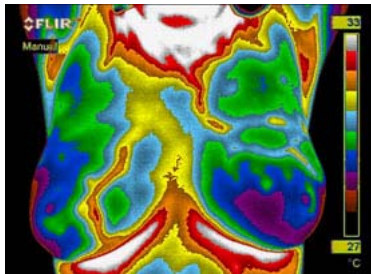


(10)

# Fractal Dimension of Ten different contours

Shape	1	2	3	4	5	6	7	8	9	10
FD	1.0711	1.1573	1.2162	1.2204	1.2750	1.2962	1.4076	1.4194	1.4370	1.4464

# Automatic segmentation of two breasts



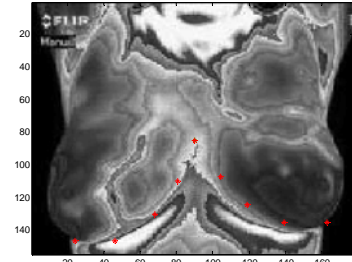
(a)



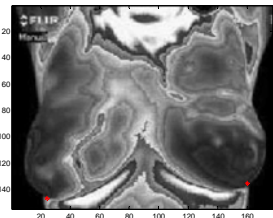
(b)



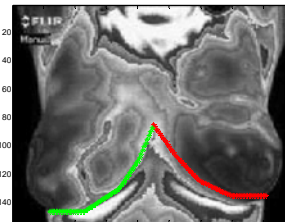
(c)



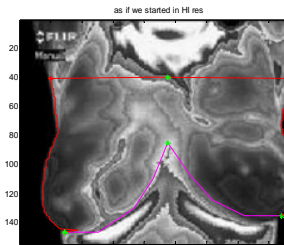
(d)



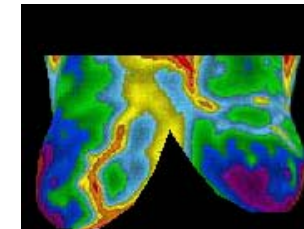
(e)



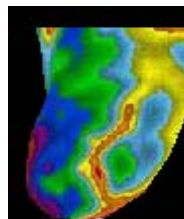
(f)



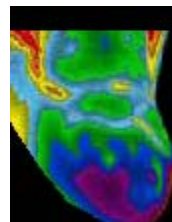
(g)



(h)



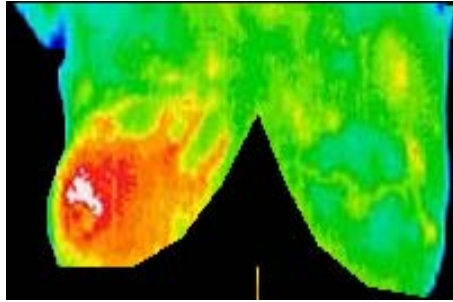
(i)



(j)

- (a) Original image, (b) output of canny edge detector, (c) Extracting outer boundaries  
 (d) 9 points with equal distances (e) two points with maximum curvature  
 (f) two lower boundaries (g) all boundaries (h) Extracting two breasts  
 (i) left breast (j) right breast

# Color segmentation by Fuzzy c means



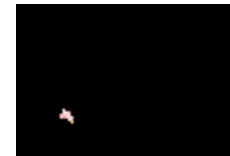
cluster 1



cluster 2



cluster 3



cluster 4



cluster 5



cluster 6



cluster 7



cluster 8



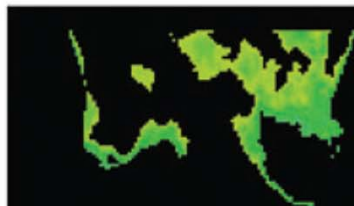
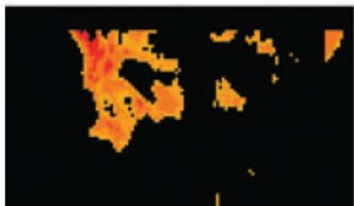
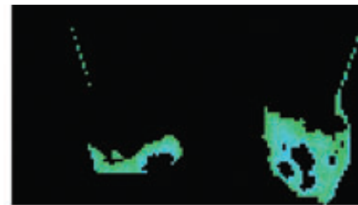
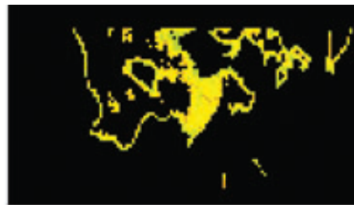
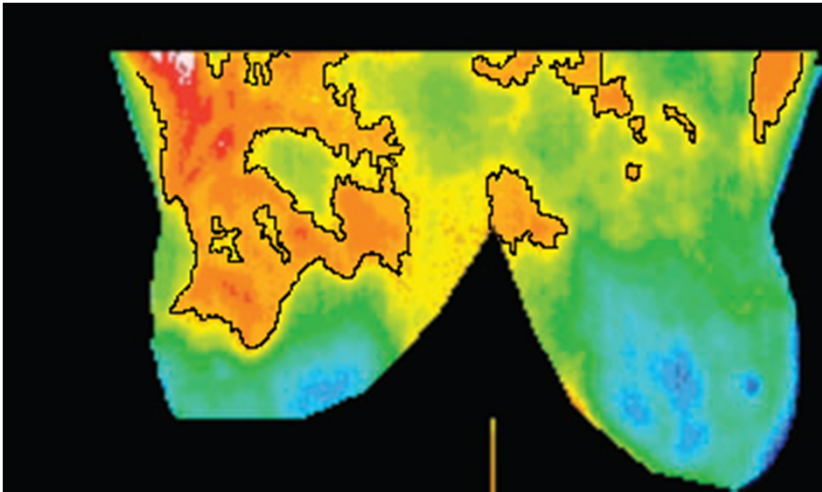
# Algorithm for detecting malignancy or benignity of breast tumors by estimating Fractal dimension

- 1) The breast IR images are segmented by fuzzy c-means
- 2) The first hottest regions are identified  
The axilla and close sternal boundaries are removed and are not considered.
- 3) The fractal dimension of step (2) is calculated with Box Counting method

# Box Counting method

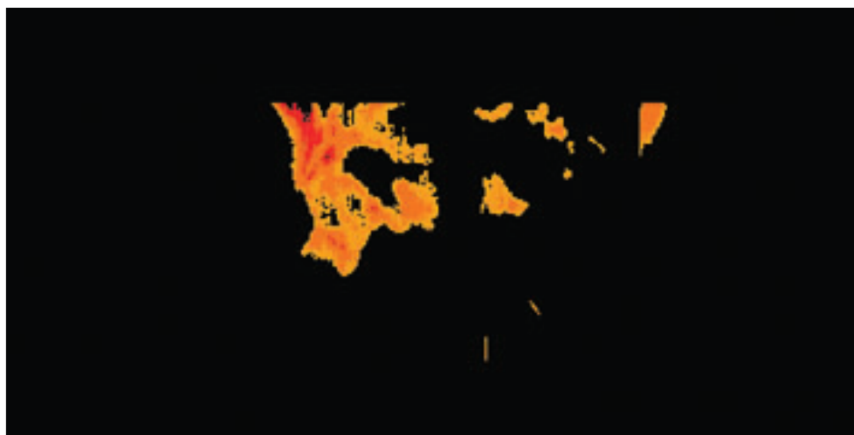
- Making the image of the first hottest regions in binary.
- Detecting the edges.
- Setting up a grid of boxes.
- Counting the number of occupied boxes.
- Changing the boxes sizes and repeating the previous step.
- Calculating the slope of the best fitting line to the plot of the log of the number of box count vs. the log of the number of boxes.

# Example

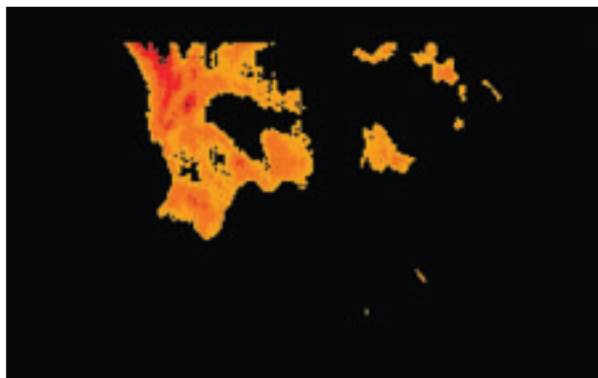


Segmentation by fuzzy c-mean





The first hottest regions



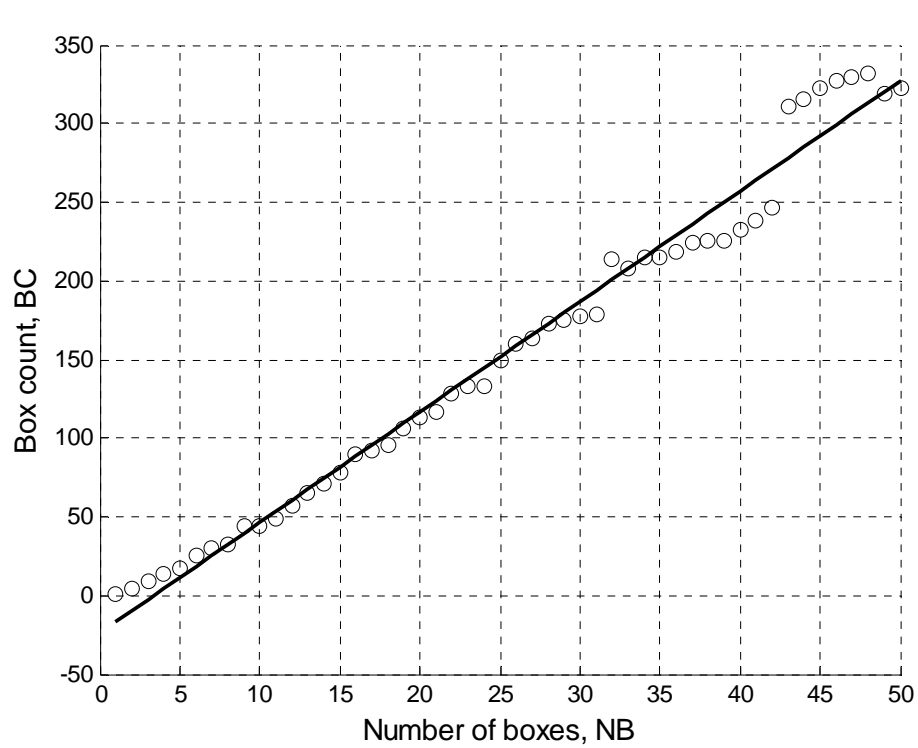
(1)



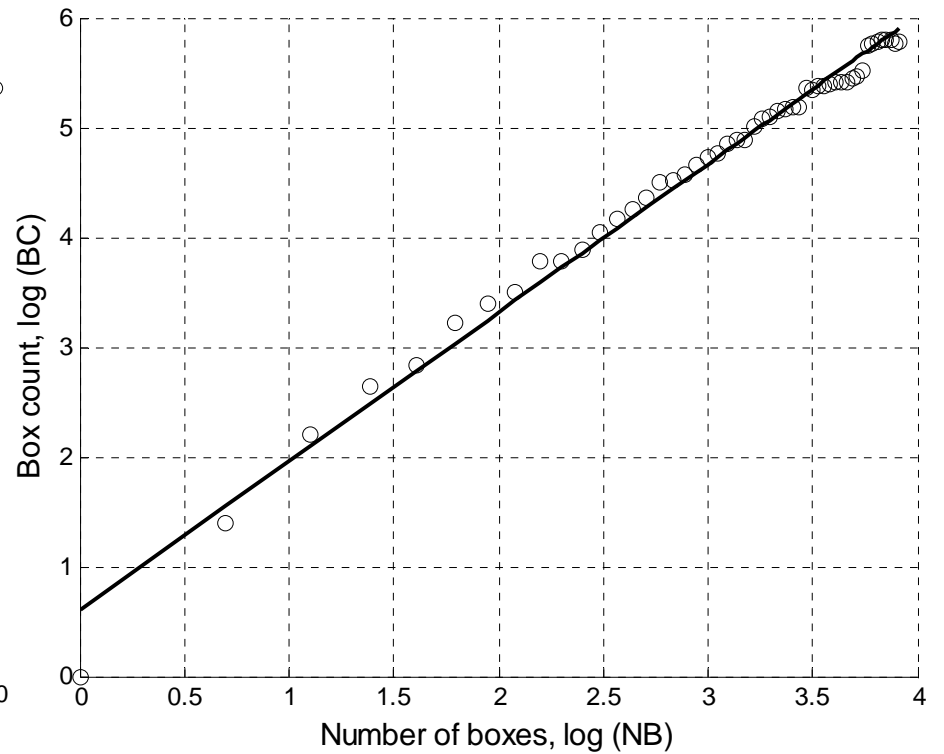
(2)

(1) The first hottest regions after removing the axilla boundaries

(2) Boundaries of part (1)



( 1 )



( 2 )

(1) Box count (BC) vs. number of boxes (NB). (2) log(BC) vs. log (NB).

When was fractals and chaos first researched? When was chaos theory relating to biology first researched?

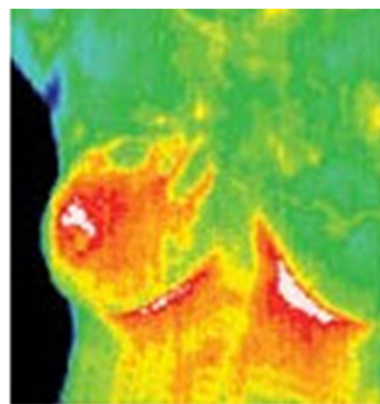
- Chaos theory relating to biology was first researched in the early 70's.
- Researchers were looking at how chaos theory could be used to model population trends.
- Several researchers, such as George Oster, Robert May, and Jim Yorke, looked at equations such as this one in their effort to model population:

$$X_{t+1} = l \cdot x_t(1 - x_t)$$

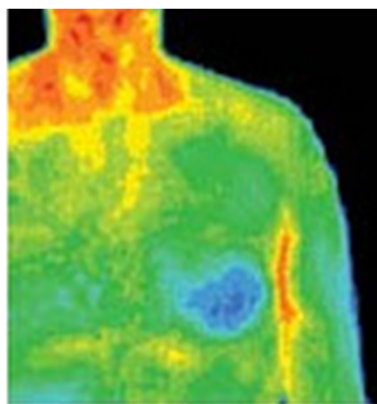
- As for human biology, shortly after the Mandelbrot Set was discovered this also took off.
- Dynamical diseases, a term coined in this era, described diseases that show chaotic systems.
- Researchers such as Leon Glass and Michael Mackey did research in this field.

# Cancer Can Grow Unpredictably

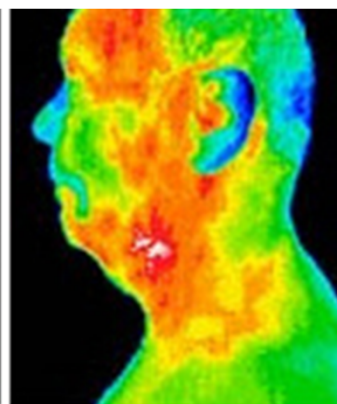
- Although cancer appears to develop in an organized fashion when viewed from the outside,
- if we were to go inside a tumor with a little magnifying glass and monitor the movement of cells and the integrity of DNA,
- we would see a much more chaotic situation.
- When the first cancer cell duplicates itself to make two cells, it also duplicates its DNA, which gets passed on to its offspring.
- As two cells become four and so on to generate the billionth cancer cell, the same DNA is duplicated over and over again (remember, a one-centimeter growth contains a billion cells).
- BUT (this is an important but!), **DNA does not remain exactly the same over the lifetime of a cancer**



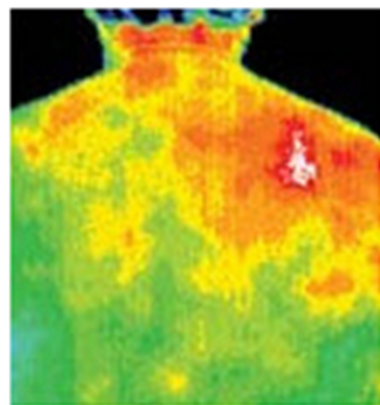
Breast Cancer



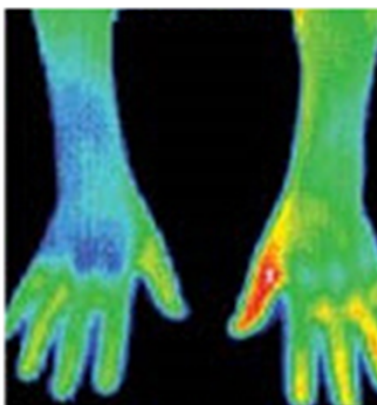
Heart Disease



Pre-Stroke



Inflammation

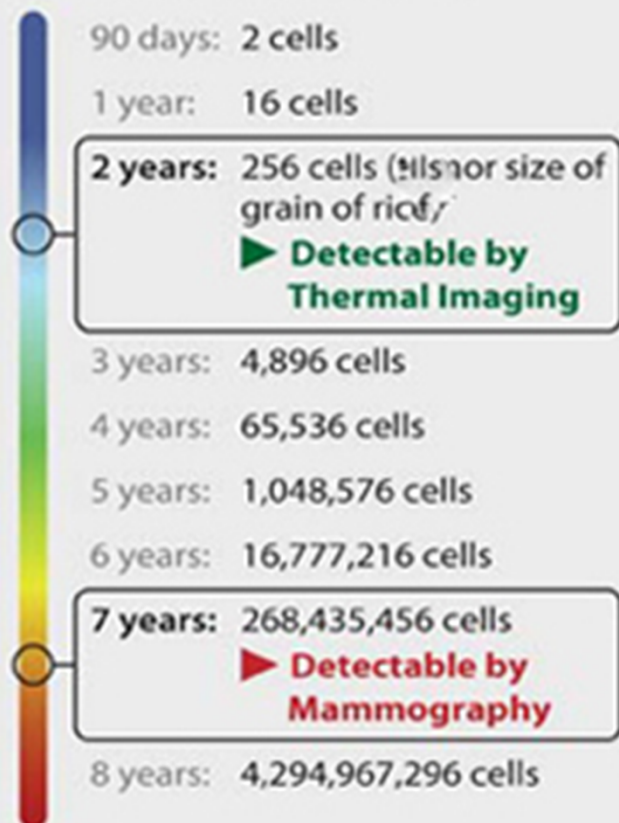


Carpal Tunnel



Periodontal

Tumors and other diseases are easily treated with early detection.



- As a cancer develops and grows, the DNA that guides it along is prone to change.
- Although the billionth cell is quite similar to the first cell (and would look the same to the pathologist under the microscope),
- its DNA may have more mutations than the first cell; because DNA determines the functions of every cell, the billionth cell may have different physical properties than the first cell.
- Thus, as a cancer grows, its genetic makeup becomes diversified, which leads to a diversity of cell types within it.
- cancer is not a collection of identical cells

- The tendency of a cancer to generate cells with different capabilities explains many of the dreadful aspects of cancer that patients find so hard to grapple with:
  - why it can spread from one location to another,
  - why it stops responding to a treatment that was working, and
  - why it can return when it was in remission.
- The reason is that every cancer, whether it arises in the lung, breast, prostate, bone marrow, fat, or elsewhere, contains different populations of cells that have distinct properties.



Stated another way, the growth of a cancer from one mutant cell is not like putting the original cell on a photocopier, setting the copy number to one billion, and walking away. A cancerous tumor, in fact, does not contain billions of identical clones. Cancer could never develop in this way because it must avoid the immune system's attack on it, live in areas of low oxygen tension, and compete with the rest of the body for vital nutrients. As these conditions change in the body, a cancer must adapt; if it fails to adapt, it is eliminated

Waldrop describes *chaos* as a nonlinear phenomenon [where]...a tiny event over *here* can have an enormous effect over *there*...the flap of a butterfly's wings in Texas could change the course of a hurricane in Haiti a week later...everything is connected and often with incredible sensitivity. Tiny perturbations won't always remain tiny. Under the right circumstance [and critical timing], the slightest uncertainty can grow until the system's future becomes utterly unpredictable...chaotic...[a] pattern of ever-increasing [disorganized] complexity

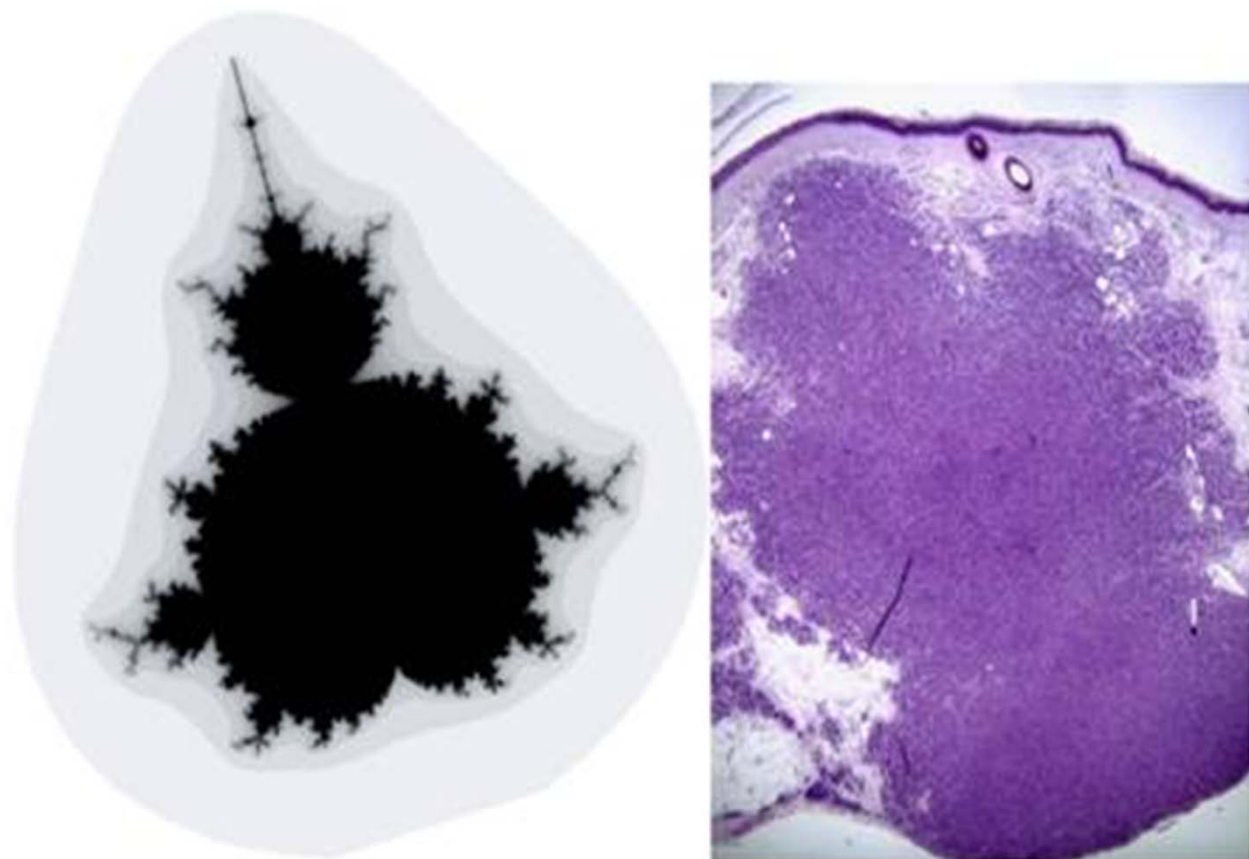
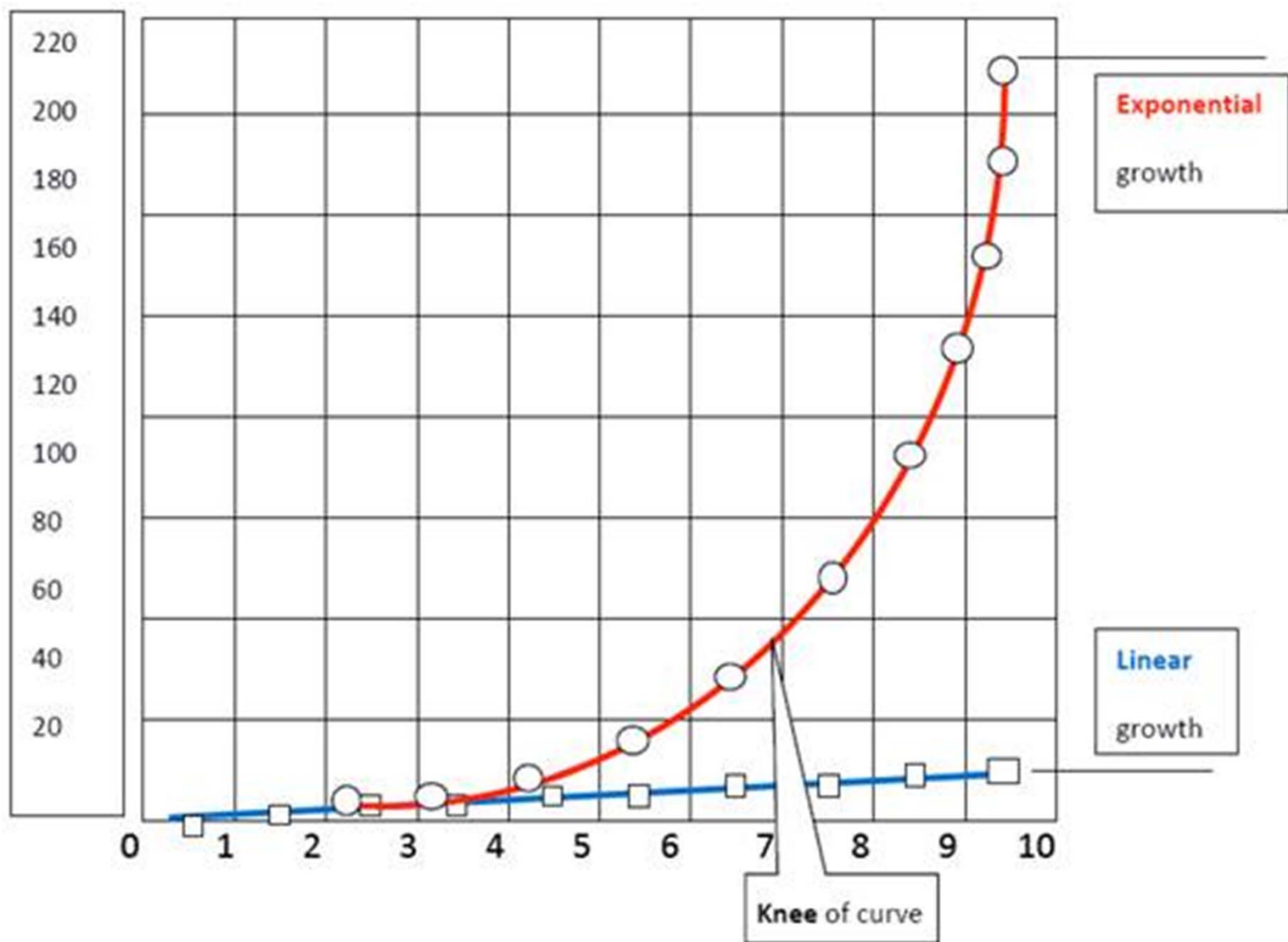


Fig. On the left is a classic Mandelbrot geometric pattern not unlike Merkel cell carcinoma on the right ([local.wasp.uwa.edu.au/.../fractals/fracintro/](http://local.wasp.uwa.edu.au/.../fractals/fracintro/) and <http://path.upmc.edu/cases/case398.html> respectively)

***Chaos*** is characterized by exponential iterations with a potential for runaway growth acceleration

. A graphic comparison of a positive exponential curve with a linear line can express the relationship between normal and malignant growth



Adopted from Kurzweil

<http://www.medsci.org/v04p0164.htm>

Cancer is a significant medical and societal problem. This reality arises from the fact that an exponential and an unrestricted cellular growth destabilizes human body as a system. From this perspective, cancer is a manifestation of a system-in-failing.

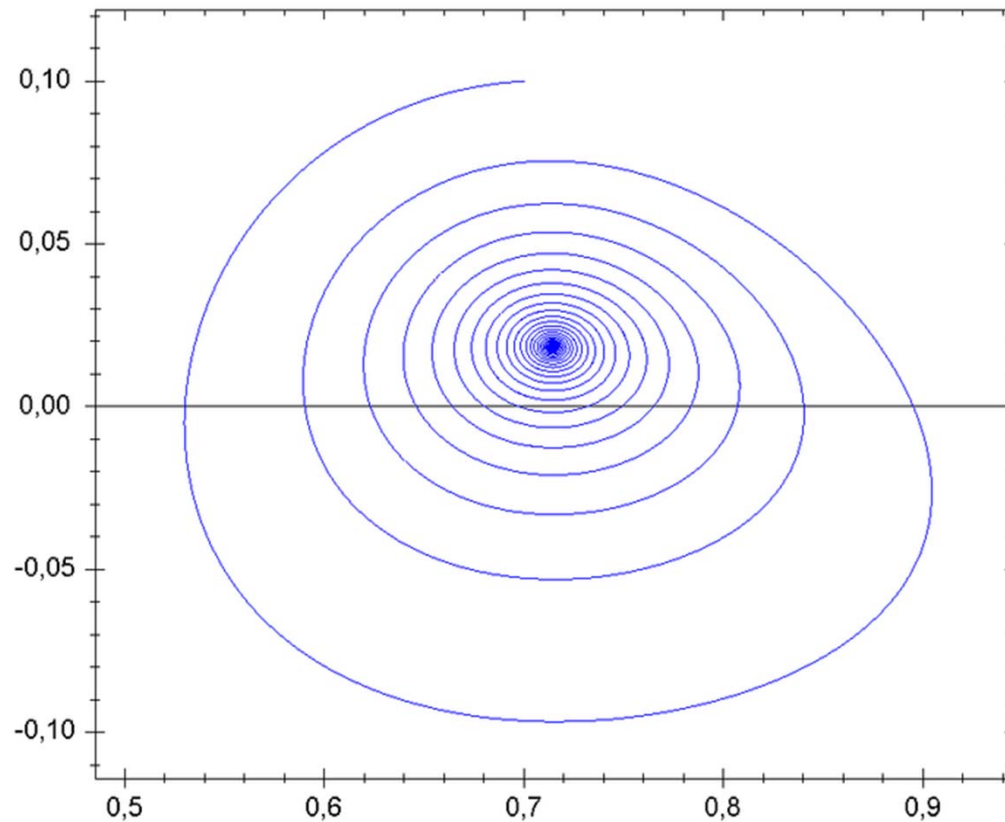
Cancerous cells, tumors, and vasculature defy have irregular shapes which have potential to be described by a nonlinear dynamical system.



- Chaotic time series (CTS) could provide the tools necessary to generate the procedures to evaluate the nonlinear system.
- Computing Lyapunov exponents (LEs) is a powerful means of quantifying the degree of the chaos.

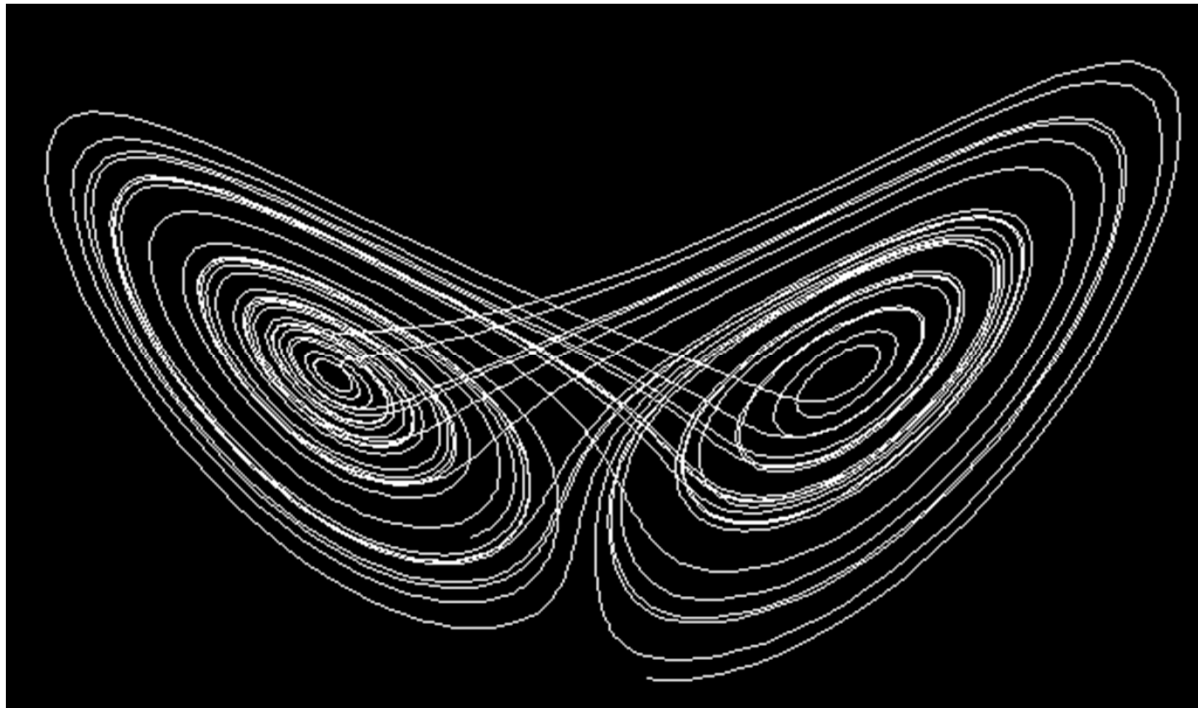
- The basic idea of CTS analysis is that an unknown complex system can be described by a strange attractor in its PS, and
- it is important to reconstruct the system state-space starting from observed time series.
- The observed time series can be seen as the output of an unknown system corrupted by noise.

A phase space, introduced is a space\_in which all possible states of a system are represented, with each possible state of the system corresponding to one unique point in the phase space.



Phase space of a dynamical system with focal stability

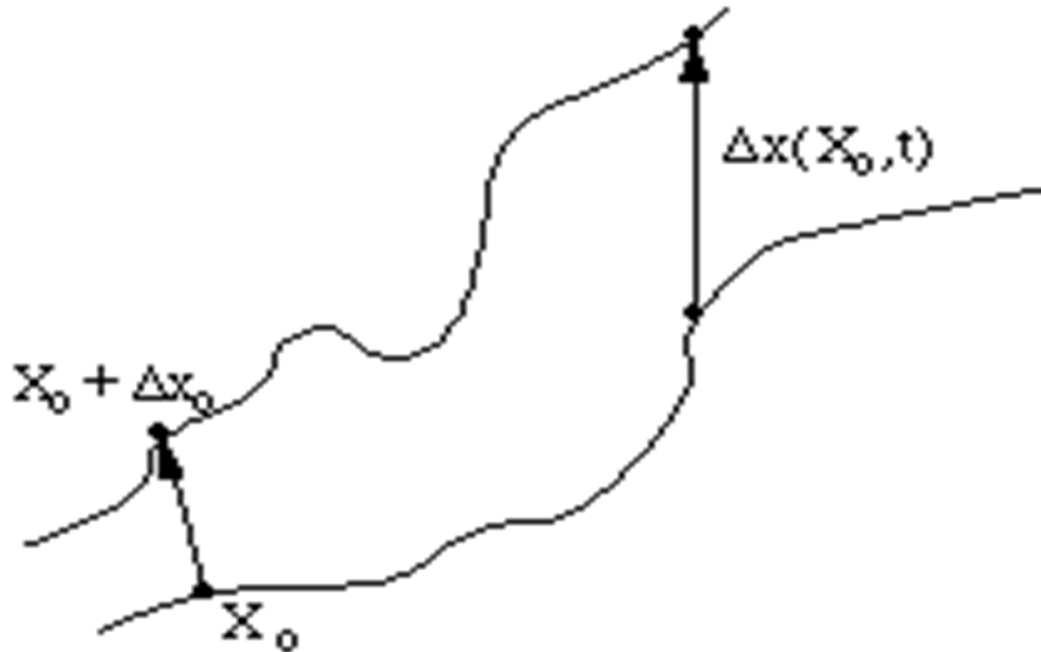
In 1961, meteorologist **Edward Lorenz** (1917-) found that extremely small changes in initial conditions had a significant effect on the weather



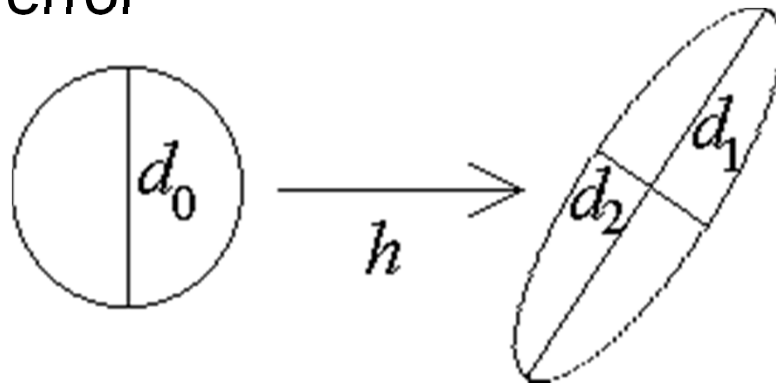
- We do not have full knowledge of the dynamics of the system because we do not have measurements for each possible variable in the system
- However, in practice, we usually have only one TS measurement. In such cases, though we cannot find the exact PS of the system, a pseudo PS (equivalent to the original PS in terms of the system invariants) may still be constructed.
- This pseudo PS is called the reconstructed phase space (RPS)

# Lyapunov exponents (LE)

The sensitive dependency on the initial conditions can be measured by LEs. It is the averaged rate of divergence or convergence of two neighboring trajectories in the PS.



- With a continuous dynamical system in  $n$  dimensional PS,
- we monitor the long term evolution of an infinitesimal  $n$  sphere initial condition where  $n$  is the number of equations (or equivalently, the number of state variables) used to describe the system.
- As time ( $t$ ) progresses, the sphere evolves into an ellipsoid whose principle axes expand (or contract) at rates given by the LEs.
- By comparing an orbit belonging to some initial condition with an orbit for an initial condition which carries an error



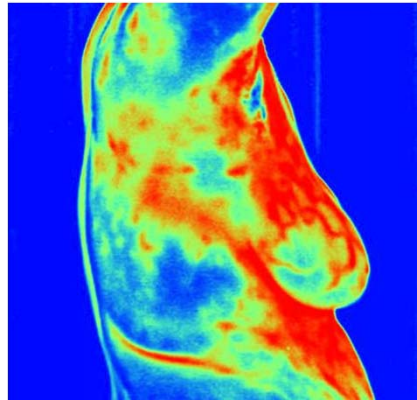
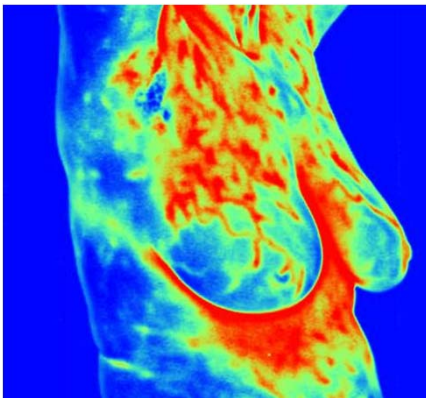
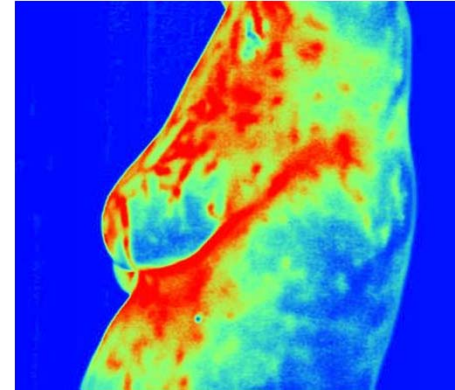
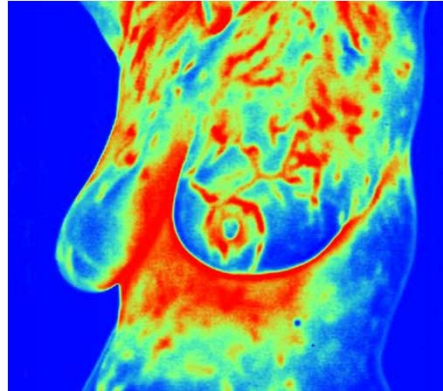
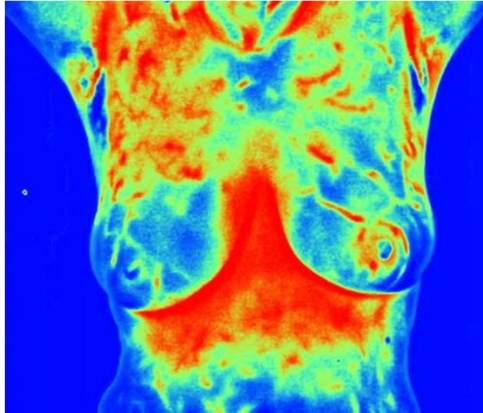
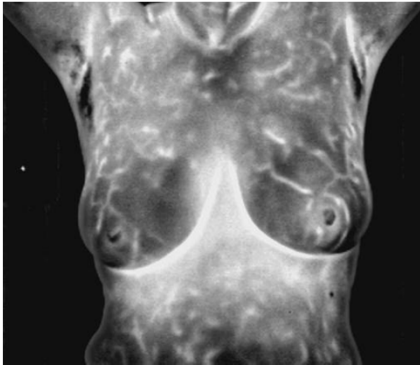
The Lyapunov exponent (LE)  
characterizes the average  
logarithmic growth of the relative  
error per iteration



Zero exponents indicate that the system is in some sort of steady state mode

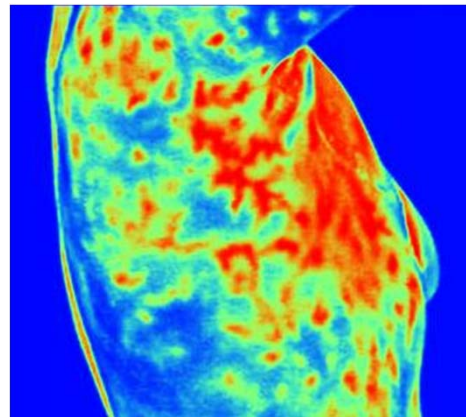
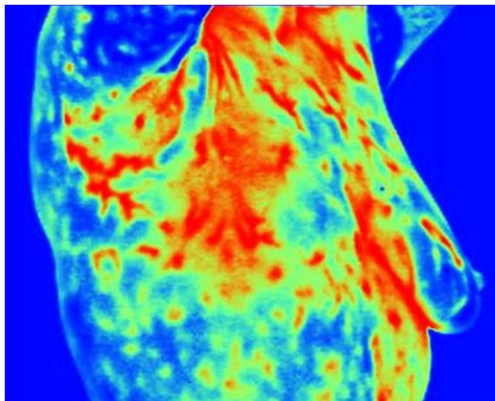
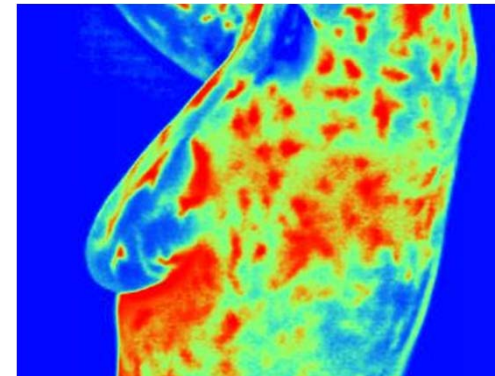
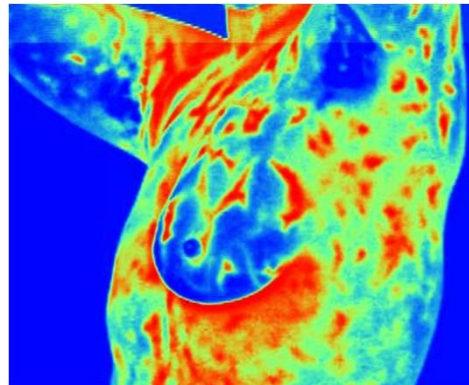
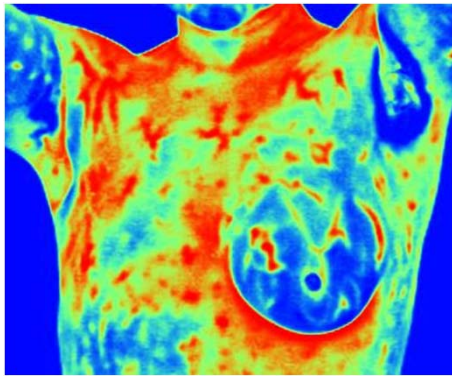
while the positive ones indicate that the system is chaotic.

# Data Collection in Seyedo Shohada Hospital in Isfahan



- Camera resolution 0.01 degree centigrade
- better room condition

# Data Collection in Seyedo Shohada Hospital in Isfahan (second time)





A high-resolution photograph of a sky filled with many white, puffy cumulus clouds. The clouds are scattered across a deep blue background, with some appearing closer and more detailed, while others are further away and more ethereal. The lighting suggests a bright, sunny day.

Thank you for your  
attention